

# HW# 4 SOLUTION

## Problem 6.10

(a) Reverse Biased - There is a deficit of minority carriers in the quasineutral immediately adjacent to the depletion region

(b) Low-level injection DOES prevail. As required for low-level injection

$$|\Delta n_p|_{\max} \cong n_{p0} \ll p_p \quad \text{for } x \leq -x_p$$

$$|\Delta p_n|_{\max} \cong p_{n0} \ll n_n \quad \text{for } x \geq x_n$$

(c) Since we have low-level injection,

$$N_A \cong p_{p0} \cong p_p = 10^{14} / \text{cm}^3$$

$$N_D \cong n_{n0} \cong n_n = 10^{15} / \text{cm}^3$$

(d) Invoking the law of the junction,

$$n(-x_p)p(-x_p) = n_i^2 e^{qV_A/kT}$$

or

$$V_A = \frac{kT}{q} \ln \left[ \frac{n(-x_p)p(-x_p)}{n_i^2} \right]$$

as deduced from Fig. P6.10,

$$n(-x_p) = 10^3 / \text{cm}^3$$

$$p(-x_p) = 10^{14} / \text{cm}^3$$

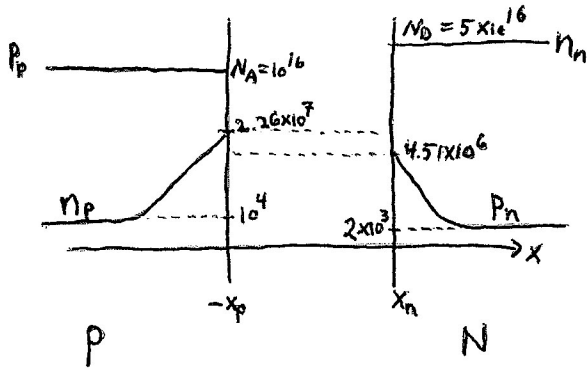
and

$$n_i = \sqrt{n(\infty)p(\infty)} = \sqrt{n(-\infty)p(-\infty)} = \sqrt{10^{20}} = 10^{10} / \text{cm}^3$$

The foregoing manipulation was necessary because the semiconductor fabricating the diode was not specified in the problem. Lastly, substituting gives:

$$V_A = (0.0259) \ln \left[ \frac{(10^3)(10^{14})}{10^{20}} \right] = \boxed{-0.18 \text{ V} = V_A}$$

2) (a) Forward Bias:



$$\frac{n_i^2}{N_A} = \frac{10^{20}}{10^{16}} = 10^4$$

$$\frac{n_i^2}{N_D} = \frac{10^{20}}{5 \times 10^{16}} = 2 \times 10^3$$

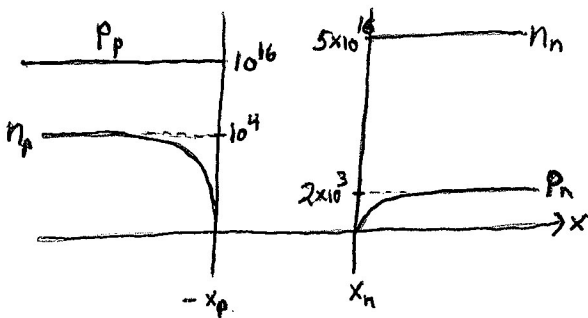
$$n_p(-x_p) = n_{p0} e^{qV_A/kT} = (10^4) e^{(0.2/0.0259)}$$

$$= 2.26 \times 10^7$$

$$p_n(x_n) = p_{n0} e^{qV_A/kT} = (2 \times 10^3) e^{0.2/0.0259}$$

$$= 4.51 \times 10^6$$

Reverse Bias:



(b)  $D_p = \frac{kT \mu_p}{q}$

$$= (0.0259)(378) = 9.79$$

$$L_p = \sqrt{D_p \tau_p} = \sqrt{9.79 \cdot 10^{-6}} = 0.00313 \text{ cm}$$

$$D_n = \frac{kT \mu_n}{q} = (0.0259)(1248) = 32.32$$

$$L_n = \sqrt{D_n \tau_n} = \sqrt{32.32 \cdot 10^{-6}} = 0.00569 \text{ cm}$$

From the graph,  $\mu_p = 378$  @  $N_D = 5 \times 10^{16}$

From the graph,  $\mu_n = 1248$  @  $N_A = 10^{16}$

$$Q_p = q A \Delta p_n L_p = (1.6 \times 10^{-19} \text{ C})(1 \text{ cm}^2)(4.5 \times 10^6)(0.00313) = 2.26 \times 10^{-15} \text{ C}$$

$$\Delta p_n = \frac{n_i^2}{N_D} (e^{qV_A/kT} - 1) = 2 \times 10^3 (e^{0.2/0.0259} - 1) = 4.5 \times 10^6$$

$$\Delta n_p = \frac{n_i^2}{N_A} (e^{qV_A/kT} - 1) = 10^4 (e^{0.2/0.0259} - 1) = 2.256 \times 10^6$$

$$Q_n = q A \Delta n_p L_n = (1.6 \times 10^{-19} \text{ C})(1 \text{ cm}^2)(2.256 \times 10^6)(0.00569) = -2.054 \times 10^{-14} \text{ C}$$

$|Q_n| \neq |Q_p|$  because  $N_D > N_A$ , so  $|Q_n| > |Q_p|$

(c)  $J_0 = q n_i^2 \left[ \frac{D_p}{N_D L_p} + \frac{D_n}{N_A L_n} \right] = (1.6 \times 10^{-19})(10^{20}) \left[ \frac{9.79}{5 \times 10^{16} \cdot 0.00313} + \frac{32.32}{10^{16} \cdot 0.00569} \right] = 1.639 \times 10^{-11} \text{ A/cm}^2$

3) (a)

$$V_A = -5V$$

$$I_{r-g} = -\frac{q A n_i^2 W}{2 \tau_0}$$

$$V_{bi} = \frac{kT}{q} \ln \left( \frac{N_A N_D}{n_i^2} \right)$$

$$= (0.0259) \ln \left( \frac{(5 \times 10^{16})(2 \times 10^{16})}{10^{20}} \right)$$

$$= 0.775V$$

$$W = \left[ \frac{2 k_s \epsilon_0}{q} \left( \frac{N_A + N_D}{N_A N_D} (V_{bi} - V_A) \right) \right]^{1/2}$$

$$= \left[ \frac{2 (11.8) (8.85 \times 10^{-14})}{1.6 \times 10^{-19}} \left( \frac{5 \times 10^{16} + 2 \times 10^{16}}{(5 \times 10^{16})(2 \times 10^{16})} (0.775 - (-5)) \right) \right]^{1/2}$$

$$W = 7.26 \times 10^{-5} \text{ cm}$$

$$\tau_0 = \frac{1}{2} (\tau_p e^{(E_T - E_i)/kT} + \tau_n e^{(E_i - E_T)/kT}) = \frac{1}{2} (\tau_n + \tau_p) = \frac{1}{2} (1 \mu s + 1 \mu s) = 1 \mu s$$

$$I \approx I_{r-g} = -\frac{q A n_i^2 W}{2 \tau_0} \quad \text{since reverse bias} > \text{few } \frac{kT}{q}$$

$$= -\frac{(1.6 \times 10^{-19})(1 \text{ cm}^2)(10^{20})}{2 (1 \times 10^{-6})} (7.26 \times 10^{-5})$$

$$I = 5.81 \times 10^{-8} \text{ A}$$

This is due to generation in the depletion region.

$$(b) \quad I_{leak} = \underbrace{q A n_i^2 \left[ \frac{D_p}{N_d L_p} + \frac{D_n}{N_a L_n} \right] \left[ e^{qV_A/kT} - 1 \right]}_{I_{diff}} + \underbrace{\frac{-q A n_i^2 W}{2 \tau_0}}_{I_{r-g}}$$

$I_{diff}$  would dominate if  $\tau_0 \gg W$  (making  $I_{r-g}$  small), or if the device has a narrow bandgap and a large  $n_i$ , so that  $n_i^2$  dominates  $n_i$ , such as Germanium.

(c) For Si,  $\epsilon_{CR} = 4 \times 10^5$

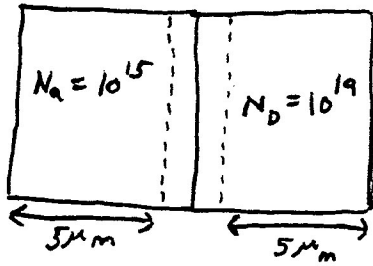
$$V_{BR} = \frac{k_s \epsilon_0 \epsilon_{CR}^2}{2 q} \frac{N_A + N_D}{N_A N_D} = \frac{(11.8)(8.85 \times 10^{-14})(4 \times 10^5)^2}{2 (1.6 \times 10^{-19})} \cdot \frac{5 \times 10^{16} + 2 \times 10^{16}}{5 \times 10^{16} \cdot 2 \times 10^{16}}$$

$$V_{BR} = 36.55 \text{ V}$$

$$(d) \quad W_{BR} = \sqrt{\frac{2 \epsilon}{q} (V_{bi} - V_{BR}) \frac{N_A + N_D}{N_A N_D}} = \sqrt{\frac{2 (11.8) (8.85 \times 10^{-14})}{1.6 \times 10^{-19}} (0.775 - (-36.55)) \frac{(5 \times 10^{16} + 2 \times 10^{16})}{5 \times 10^{16} \times 2 \times 10^{16}}}$$

$$W_{BR} = 1.847 \times 10^{-4} \text{ cm}$$

4)



$$\mu_n = 1345 \text{ @ } N_A = 10^{15}$$

$$\mu_p \approx 60 \text{ @ } N_D = 10^{19}$$

$$D_n = \frac{kT}{q} \mu_n = (0.0259)(1345) = 34.84$$

$$L_n = \sqrt{D_n \tau_n} = \sqrt{(34.84)(1 \mu s)} = 5.902$$

$$D_p = \frac{kT}{q} \mu_p = (0.0259)(60) = 1.554$$

$$L_p = \sqrt{D_p \tau_p} = \sqrt{(1.554)(10^{-6})} = 1.247 \times 10^{-3}$$

Since  $N_D \gg N_A$ , assume most of the voltage drop occurs on the P side of the diode.

$$\rho = \frac{1}{q \mu_p N_A} = \frac{1}{(1.6 \times 10^{-19})(60)(10^{15})} = 104.17 \Omega \cdot \text{cm}$$

$$R = \frac{\rho l}{A} = \frac{(104.17)(5 \mu\text{m})}{A} = 5.21 \frac{\Omega}{A}$$

$$V = IR \Rightarrow 0.1 \text{ V} = I (5.21/A)$$

$$I = q A n_i^2 \left[ \frac{D_p}{N_A L_p} + \frac{D_n}{N_D L_n} \right] \left[ e^{qV/kT} - 1 \right]$$

$$= (1.6 \times 10^{-19}) A (10^{10})^2 \left[ \frac{1.554}{10^{19}(1.247 \times 10^{-3})} + \frac{34.84}{10^{15}(5.902)} \right] \left[ e^{qV/kT} - 1 \right]$$

$$I = (94.44 \text{ A}) \left[ e^{qV/kT} - 1 \right] \times 10^{-12}$$

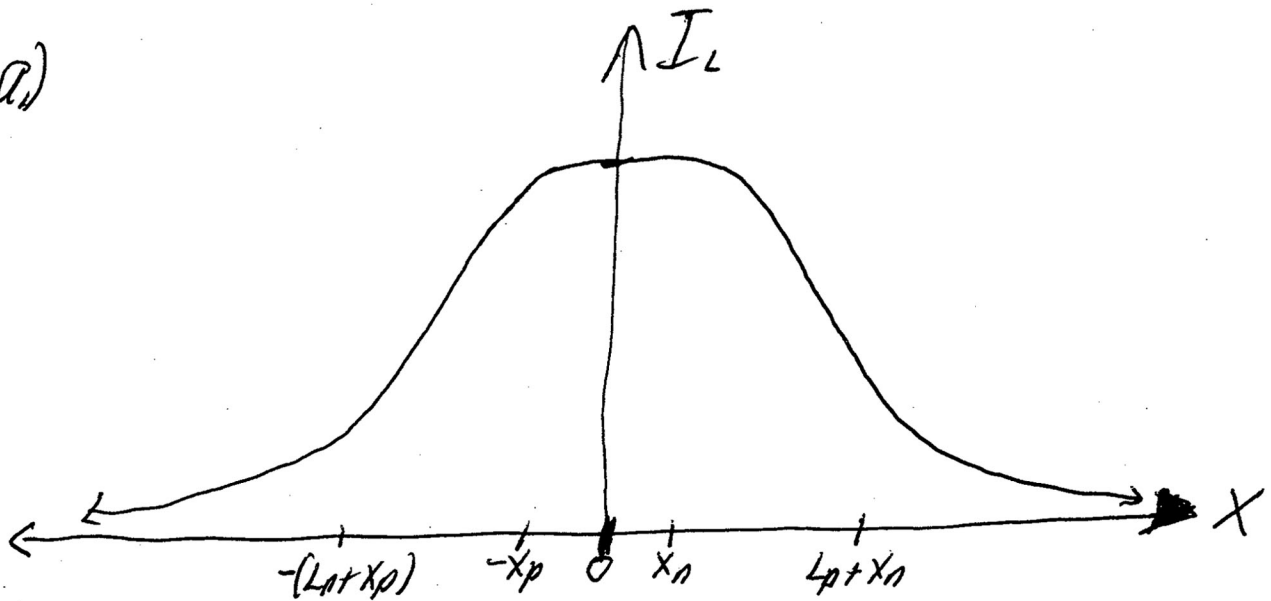
$$0.1 \text{ V} = V = IR = (94.44 \text{ A}) (5.21/A) \left[ e^{qV/kT} - 1 \right] \times 10^{-12}$$

$$\Rightarrow e^{qV/kT} - 1 = 2.033 \times 10^8$$

$$\Rightarrow V_A = \ln(2.033 \times 10^8 + 1) (0.0259) = 0.495 \text{ V}$$

Using this value,  $J_{\text{gen}} \approx 9.76 \times 10^{-15} \sim 0$ , so that term can be reasonably ignored in this case.

5) a)



All light absorbed in depletion region is useful photocurrent, light outside depletion region produces minority carriers that may not be able to diffuse to the depletion region (and swept to their majority region) before recombination. The lengths for the diffusion process are  $\sim L_n, L_p$

b) 
$$I = \frac{q n_i}{2\tau_0} A W \quad \text{reverse bias no light}$$

$$I_L = \frac{q A G_L (W + L_n + L_p)}{\downarrow} \quad \text{for uniform light across junction}$$
  
 generated over a volume of  $1\mu\text{m} \times 1\mu\text{m} \times 10\mu\text{m}$

For this device, the light dictates the volume,  $\therefore A(W + L_n + L_p)$  is irrelevant

$$I_L = q G_L (1\mu\text{m} \times 1\mu\text{m} \times 10\mu\text{m})$$

$$I_L = .16 \text{ pA}$$

light on

$$I = \frac{q n_i}{2\tau_0} A W \quad W = \sqrt{\frac{2 \epsilon_s N_A N_D}{q} V_{bi}}$$

$$V_{bi} = \frac{kT}{q} \ln \frac{N_A N_D}{n_i^2} = .71 \text{ V}$$

$$W = .43 \mu\text{m}$$

$$I_{\text{OFF}} = .38 \text{ pA}$$

We assume here that  $V_A$  is not large enough to cause an enormous change from  $W$ 's equilibrium value; without a value for  $V_A$  given,  $V_{bi}$  suffices to get an estimate.

The light is too narrow & dim to dominate! (But it can still be detected, of course.)