

Spring 2012 : Transmission Lines, Fields & Waves

Solution

(a) VSWR $\Gamma_L = \frac{Z_L - 1}{Z_L + 1} = \frac{0.8 - j0.6 - 1}{0.8 + j0.6 + 1} = -j0.333$

$$Z_L = \frac{40 - j80}{50} = 0.8 - j0.6$$

$$S = \frac{1 + |\Gamma|}{1 - |\Gamma|} = \underline{\underline{2}} \quad (0.5 \text{ VSW})$$

(b) $f\lambda = v$, $\lambda = \frac{1 \times 10^8}{1 \times 10^8} = 1 \text{ m}$
 $Z_L = 0.8 - j0.6$ & $Y_L = \frac{1}{Z_L} = 0.8 + j0.6$

From Smith Chart. line length to intersect with admittance $1 + j0$ circle is $\approx 0.025\lambda$
 $= \underline{\underline{0.025 \text{ m}}}$

$$Y_L' = 1.0 + j0.7$$

Use short circuit stub length $-j0.7$
 at $50 \Omega Z_0 = 0.1525\lambda$
 $= \underline{\underline{0.1525 \text{ m}}}$

(c) Use the Smith Chart again

$$\lambda = \frac{1 \times 10^8}{9 \times 10^7} = 1.111 \text{ m}$$

$$Z_L = 0.8 - j0.666, Y_L = 0.74 + j0.62$$

Rotate towards generator by $\frac{0.025\lambda}{1.111}$

$$\text{equiv } Y_{L2} = 0.88 + j0.85$$

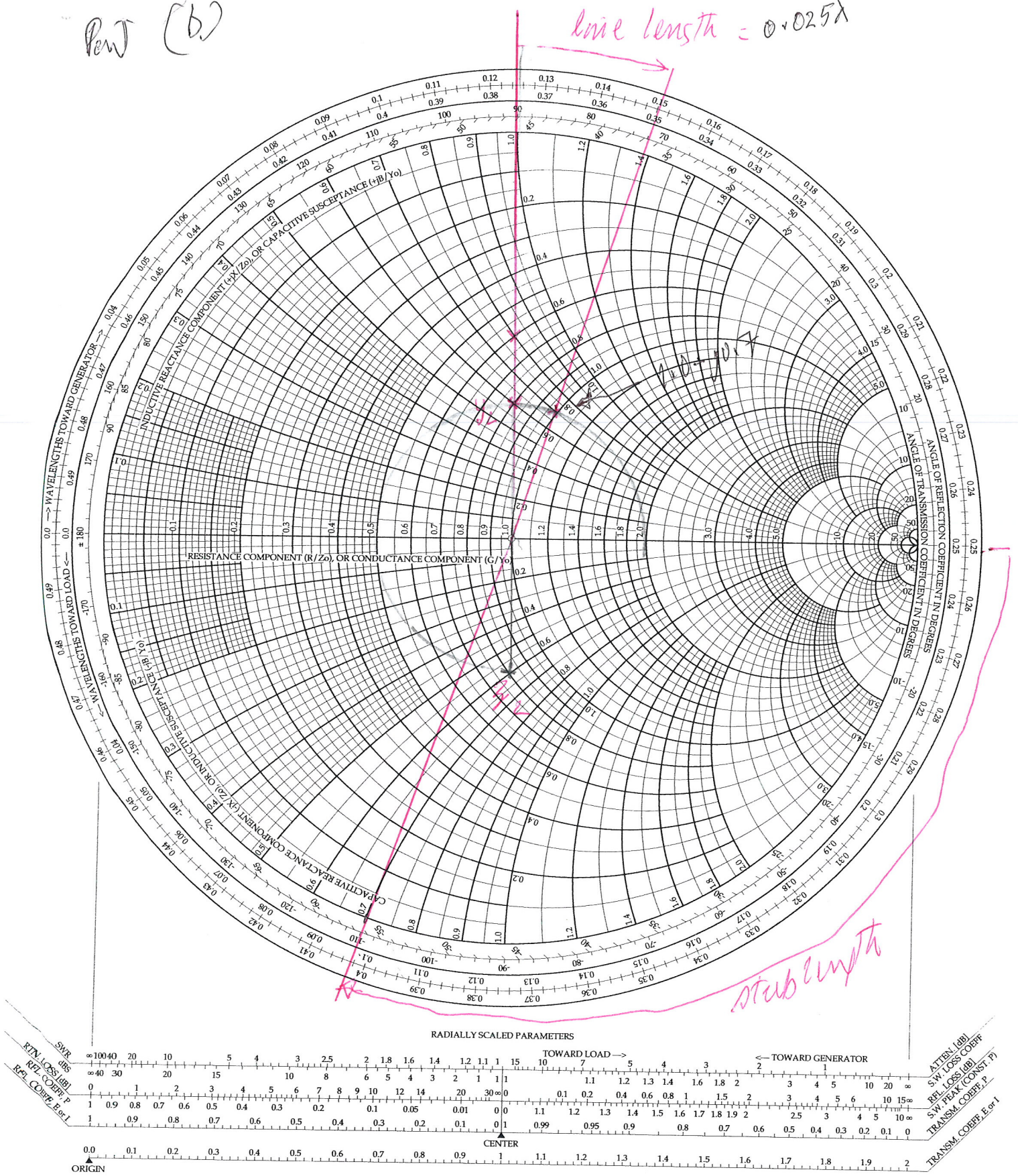
$$\text{Stub length} = \frac{0.1525}{1.111} = 0.137\lambda$$

$$\text{Short circuit stub of this length } jB_{\text{stub}} = -j0.85$$

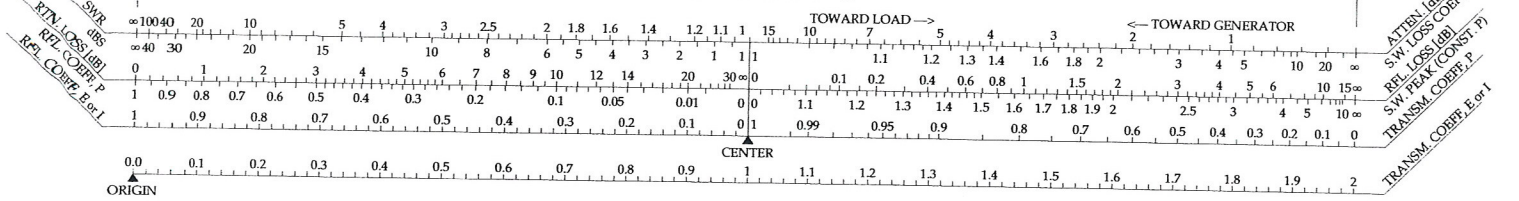
$Y_{in} = 0.88$
 $Z_{in} = 58.8 \Omega$

Pew (b)

line length = 0.025λ



RADIALLY SCALED PARAMETERS



Part (c)

0.0225λ

0.88 - j0.85
-j0.85

∠ = 0.88
Z_{in} =

Stub = 0.137λ

-j0.85

