

Solutions

$$V_0 = \frac{kT}{q} \left[\ln \frac{N_A N_D}{n_i^2} \right]$$

$$= 0.0259 \left[\ln \frac{N_A \cdot N_D}{\{1.5 \times 10^{10}\}^2} \right] = 0.6946 \text{ V}$$

$$\ln \frac{N_A \cdot N_D}{\{1.5 \times 10^{10}\}^2} = 26.82$$

$$\frac{N_A \cdot N_D}{\{1.5 \times 10^{10}\}^2} = e^{26.82} \Rightarrow N_A \cdot N_D = 1.0 \times 10^{32} \quad [\text{cm}^{-6}]$$

$$\Rightarrow N_D = 1.0 \times 10^{32} / N_A \quad \textcircled{1}$$

$$W = \sqrt{\frac{2k_s \epsilon_0}{q} \left(\frac{1}{N_D} + \frac{1}{N_A} \right) V_0} = 9.6 \times 10^{-5} \text{ cm}$$

$$\frac{2 \cdot 11.8 \cdot 8.85 \times 10^{-14}}{1.6 \times 10^{-19}} \left(\frac{1}{N_D} + \frac{1}{N_A} \right) \cdot 0.6946 = (9.6 \times 10^{-5})^2 \text{ cm}$$

$$\frac{1}{N_D} + \frac{1}{N_A} = 1.01 \times 10^{-15} \quad [\text{cm}^3] \quad - \textcircled{2}$$

$$\text{From } \textcircled{1} \text{ and } \textcircled{2}, \quad \frac{N_A}{1.0 \times 10^{32}} + \frac{1}{N_A} = 1.01 \times 10^{-15}$$

$$\Rightarrow N_A = 10^{15} \text{ cm}^{-3}, \quad N_D = 10^{17} \text{ cm}^{-3} \quad (\because N_D > N_A)$$

Forward bias current

$$I = A \cdot J_0 \left(e^{\frac{qV_A}{kT}} - 1 \right) \quad - \textcircled{3}$$

Solutions

PhD Preliminary Written Exam
Spring 2014

Problem 6
Semiconductor Devices

Page 2 of 3

$$J_0 = (q \cdot n_i^2) \left[\frac{D_p}{N_D L_p} + \frac{D_n}{N_A L_n} \right]$$

$$D_p = \mu_p \frac{kT}{q}$$

↑ hole diffusion coefficient (cm²/sec)

μ_p : hole mobility (cm²/V.s)

$$\mu_p = \underline{331 \text{ cm}^2/\text{V.s}} \quad \text{for } N_D = 10^{17} \text{ cm}^{-3}$$

see graph below

$$D_p = 331 \times 0.0259 = 8.5729 \text{ cm}^2/\text{s}$$

$$D_n = \mu_n \frac{kT}{q}$$

$$\mu_n = \underline{1345 \text{ cm}^2/\text{V.s}} \quad \text{for } N_D = 10^{15} \text{ cm}^{-3}$$

see graph below

$$D_n = 1345 \cdot 0.0259 = 34.836 \text{ cm}^2/\text{s}$$

$$L_p = \sqrt{D_p \tau} = \sqrt{8.5729 \times 0.0025} = 0.146 \text{ cm}$$

↑ Diffusion length for holes

$$L_n = \sqrt{D_n \tau} = \sqrt{34.836 \times 0.0025} = 0.295 \text{ cm}$$

$$J_0 = 1.6 \times 10^{-19} \cdot (1.5 \times 10^{10})^2 \cdot \left[\frac{8.5729}{10^{17} \cdot 0.146} + \frac{34.836}{10^{15} \cdot 0.295} \right]$$

$$= 4.27 \times 10^{-12} \text{ C/cm}^2 \cdot \text{s}$$

$$I = A \cdot J_0 \left(e^{\frac{qVA}{kT}} - 1 \right) = 0.001 \times 4.27 \times 10^{-12} \times \left(e^{\frac{0.65}{0.0259}} - 1 \right)$$

$$= 0.3386 \text{ mA}$$

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PhD Preliminary Written Exam
Spring 2014

Problem 6
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Page 3 of 3

