

# Qualifying Exam Fall 2011: Transmission Lines, Fields and Waves

Note that  $\epsilon_0 = 8.8542 \cdot 10^{-12}$  F/m, and  $\mu_0 = 4\pi \cdot 10^{-7}$  H/m.

1. (a) The reflection coefficient at the input gate of a microwave FET in the grounded source configuration, is measured as  $0.3 \angle -25^\circ$  in a  $50\Omega$  transmission line system at 6 GHz, with the transmission line velocity  $1 \times 10^8$  m/sec.
  - i. At what distance in wavelengths and cms, nearest to the gate is the voltage minimum along this line? (Use a Smith Chart) (0.5 points)
  - ii. What is the input impedance in ohms at this voltage minimum? (0.5 points)
  - iii. Design a quarter-wave transformer matching circuit for the input gate of this device to  $50\Omega$  from this voltage minimum. (1 point)
  
- (b) With crude oil prices of over \$80 per barrel, extraction of oil from shale is an economic proposition. In one such procedure, a coaxial line with slots is placed in a borehole, and radiates at 915 MHz into the shale, to separate the oil and water from the soil. Assume that the  $\epsilon_r$  of wet oil loaded shale is 25.5 and  $\sigma$  is 0.5 S/m, and also assume **plane wave propagation**.
  - i. What is the complex permittivity  $\epsilon_c$  of the shale? (0.5 points)
  - ii. What is the skin depth of the medium? 0.5 points)
  - iii. What is the attenuation in dB/m in the direction away from the borehole? (0.5 points)
  - iv. Determine the the distance at which the radiated power decays to an electric field value of  $10 \mu\text{V/cm}$  if the initial power density in the soil at the edge of the borehole is  $2.75\text{KW/m}^2$ . (0.5 points)

# Smith Chart

