

# Solution Prob 9(a) Power Systems

$$i) \quad P_{load} = 500 \text{ mw} = 5 \text{ pu}$$

$$Q_{load} = 0 = 0 \text{ pu}$$

$$5 + j0 = -V \angle \theta \cdot I_L^*$$

$$= -V \angle \theta \left( \frac{V \angle \theta - 1}{.1j} \right)^* = -V \angle \theta \left( \frac{V \angle -\theta - 1}{-.1j} \right)$$

$$= \frac{V^2 - V \angle \theta}{.1j} = -10j \left( V^2 - V \cos \theta - V \sin \theta j \right)$$

$$= -10V^2 j + 10V \cos \theta j - 10V \sin \theta$$

So  $P = -10V \sin \theta$  or  $5 = -10V \sin \theta$

$Q = 10V(\cos \theta - V)$  so  $V = \cos \theta$

Then  $-.5 = V \sin \theta$  or  $-.5 = \cos \theta \sin \theta$

Answer  $\theta = -\pi/4$  or  $-45^\circ$

Then  $V = .707$

$$ii) \quad I_{gen} = \frac{1 - V \angle \theta}{.1j}$$

$$P_{gen} + jQ_{gen} = 1 \left( I_L \right)^* = 1 \left( \frac{1 - V \angle \theta}{-.1j} \right)$$

$$= \frac{1 - .707(\cos(+45^\circ) + j \sin(+45^\circ))}{-.1j}$$

Prob 9a solution

ii) cont)

$$P_{gen} + jQ_{gen} = 10j(1 - .5 - .5j)$$

$$= 10j(.5 - .5j) = 5 + 5j$$

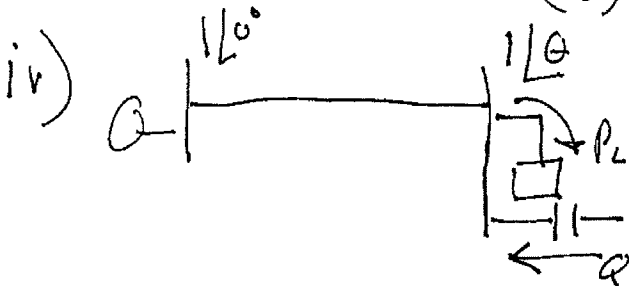
So  $P_{gen} = 5$       or  $P_{gen} = 500 \text{ MW}$   
 $Q_{gen} = 5$        $Q_{gen} = 500 \text{ MVAR}$

iii) if  $Q_{load} = 0$  then  $Q_{gen} = Q_{line} = 5 \text{ pu} = 500 \text{ MVAR}$

also  $I_L = \frac{1 - V/\theta}{.1j} = -10j(1 - .5 + .5j)$

$$= -10j + 5j + 5 = 5 - 5j$$

Then  $Q_{line} = (I_L)^2 X = (25 + 25) \cdot 1 = 50(1) = 5 \text{ pu}$



let  $I_L =$  net current into Bus from load + cap.

$$I_L = \frac{1\angle\theta - 1}{.1j} = -10j(1\angle\theta - 1)$$

$$P_{net} + jQ_{net} = -1\angle\theta \left( \frac{1\angle\theta - 1}{.1j} \right)^* = \frac{1 - 1\angle\theta}{.1j}$$

$$= -10j(1 - 1\angle\theta)$$

# Prob 9a Solution cont.

iv) continued

$$\begin{aligned}P_{\text{net}} + jQ_{\text{net}} &= -10j(1 - (\cos\theta + jsin\theta)) \\ &= -10j(1 - \cos\theta - jsin\theta) \\ &= -10j + 10j\cos\theta - 10sin\theta\end{aligned}$$

$$P_{\text{net}} = 5 = -10sin\theta, \quad sin\theta = -0.5, \quad \theta = -30^\circ$$

$$Q_{\text{net}} = -10 + 10\cos\theta = -10 + 10(0.866) = -1.339$$

Then the capacitor must inject 1.339 pu var  
or 133.9 MVAR  
into the bus.

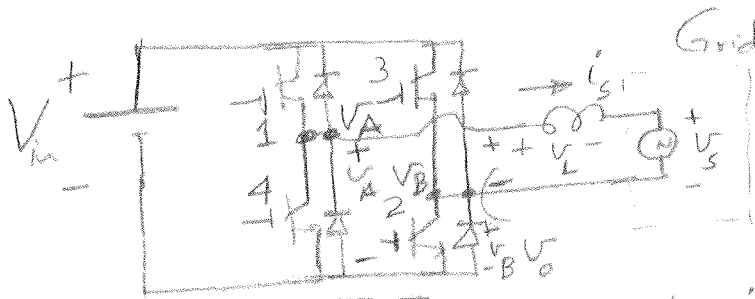
# Solution of

November 10, 2012 Problem 9(b) Power Electronics

page 1 of 2

(2 pts) In a photovoltaic system, the voltage of the PV panel is first boosted to 250V across a capacitor. An inverter is used to interface this input dc voltage  $V_m = 250V$  to the single-phase ac grid, whose sinusoidal voltage is  $\bar{V}_s = 120 \angle 0^\circ V (rms)$  at 60 Hz. The power supplied to the grid is 500W at a unity power factor (assuming the ripple in the ac-side current to be negligible). At this operating condition, the inductor  $L_s$  between the inverter and the ac grid is such that the voltage drop across this inductor is  $V_L = 5V (rms)$ . Assume ideal components and the switching frequency to be much higher than 60 Hz.

Draw the inverter circuit consisting of IGBTs and diodes, label the IGBTs from one to four, and then calculate and draw the duty-ratios of the four IGBTs as a function of  $\omega t$ . Label your graphs.



@ unity PF  $P = \bar{V}_s \bar{I}_s = 500W \therefore \bar{I}_s = \frac{500}{120} = 4.167 \angle 0^\circ A$

$\bar{V}_L = j\omega L_s \bar{I}_s = 5.0 \angle 90^\circ$

$\therefore \bar{V}_0 = \bar{V}_s + \bar{V}_L = 120 \angle 0^\circ + 5.0 \angle 90^\circ \approx 120.1 \angle 2.4^\circ V$

$\bar{V}_A = \frac{V_{in}}{2} + \frac{\bar{V}_0}{2}, \bar{V}_B = \frac{V_{in}}{2} - \frac{\bar{V}_0}{2} \therefore \bar{V}_0 = 169.85 \cos(\omega t + 2.4^\circ)$

$\therefore \bar{V}_A = 125 + 84.92 \cos(\omega t + 2.4^\circ) V$

$\bar{V}_B = 125 - 84.92 \cos(\omega t + 2.4^\circ)$

$\therefore d_1 = \bar{V}_A / V_{in} = \frac{1}{2} + \frac{84.92}{250} \cos(\omega t + 2.4^\circ) \approx 0.5 + 0.34 \cos(\omega t + 2.4^\circ)$

$d_3 = \bar{V}_B / V_{in} \approx 0.5 - 0.34 \cos(\omega t + 2.4^\circ); d_2 = 1 - d_3 = d_1$   
and  $d_4 = 1 - d_1 = d_3$

