

A. The diode equations are

$$J_1 = J_{sc,1} - J_{01} (e^{v/v_T} - 1)$$

parallel:

$$J_{||} = \underbrace{(J_{sc,1} + J_{sc,2})}_{36 \text{ mA/cm}} - (J_{01} + J_{02}) (e^{v/v_T} - 1)$$

Use v_{oc} to get $J_{0i} = \frac{J_{sc,i}}{e^{v_{oc,i}/v_T} - 1}$

$$J_{01} = 8.26 \times 10^{-8} \text{ mA/cm}^2$$

$$J_{02} = 1.39 \times 10^{-9} \text{ mA/cm}^2$$

$$v_{oc,||} = v_T \ln \left(\frac{36}{J_{01} + J_{02}} + 1 \right)$$

$$\underline{v_{oc,||} = 0.515 \text{ V}}$$

In series, at open circuit $v_{oc} = v_{oc1} + v_{oc2}$.
at short circuit $v_1 = -v_2$

$$I_{sc1} - I_{o1} (e^{-v_2/v_T} - 1) = I_{sc2} - I_{o2} (e^{v_2/v_T} - 1)$$

Expect cell 1 to be slightly forward biased to match currents, i.e. $v_2 < 0$

$$I_{sc1} - I_{o1} e^{-v_2/v_T} = I_{sc2} + I_{o2}$$

$$-v_2 = V_T \ln \frac{I_{sc2} + I_{o2}}{I_{o1}}$$

$$v_2 = -0.458$$

$$I_{sc||} = I_{sc,2} - I_{o2} (e^{.458/v_T} - 1) = 15.93$$

$$=$$

$$I_{sc||} = 16 \text{ mA as expected (weak link)}$$

B.) With an applied voltage V_a

$$\cancel{\phi_{\text{graphene}}} + V_{ox} + \phi_s = V_a + \cancel{\phi_s}$$

$$V_{ox} = \frac{Q_{\text{dupl}}}{C_{ox}} = \frac{q N_A W x_0}{K_0 \epsilon_0}$$

$$V_a = \phi_s + \frac{q N_A x_0}{K_0 \epsilon_0} \left(\frac{2 K_S \epsilon_0}{q N_A} \right)^{1/2} \phi_s^{1/2}$$

$$V_a = 100 = \phi_s + 1.59 \phi^{1/2}$$

$$\phi_s = 100 - 1.59 \phi^{1/2}$$

iterate a few times

$$\phi_s = 85.3 \Rightarrow V_{ox} = \frac{100 - 85.3}{1}$$

$$\xi = \frac{14.7}{x_0} = 4.90 \times 10^5 \text{ V/cm}$$

In accumulation, $\xi = \frac{100}{x_0}$