

SOLUTION

$$\vec{B} = (0 \mid 0 \mid B_z) \quad \vec{E} = (E_x \mid E_y \mid 0)$$

$$\vec{B} \cdot \vec{E} = 0 \quad \vec{E} \times \vec{B} = (E_y B_z \mid -E_x B_z \mid 0)$$

$$j_z = 0$$

$$j_x = \epsilon_0 \left[(1 - \mu^2 B_z^2) E_x - \mu B_z E_y \right]$$

$$j_y = \epsilon_0 \left[(1 - \mu^2 B_z^2) E_y + \mu B_z E_x \right] = 0$$

$$\rightarrow E_x = - \frac{1 - \mu^2 B_z^2}{\mu B_z} E_y$$

$$\rightarrow j_x = -\epsilon_0 \left[\frac{(1 - \mu^2 B_z^2)^2}{\mu B_z} + \mu B_z \right] E_y$$

$$E_y = - \left(\frac{j_x}{\epsilon_0} \right) \left[\frac{1}{(1 - \mu^2 B_z^2)^2 \frac{1}{\mu B_z} + \mu B_z} \right]$$

$$= - \left(\frac{j_x}{\epsilon_0} \right) \mu B_z \frac{1}{(1 - \mu^2 B_z^2)^2 + \mu^2 B_z^2}$$

to 1st order in B :

$$E_y = - \left(\frac{j_x}{\epsilon_0} \right) \mu B_z$$

$$\bar{E}_x = + \frac{1 - \mu^2 \beta_z^2}{\mu \beta_z} \left(\frac{j_x}{\epsilon_0} \right) \mu \beta_z \frac{1}{(1 - \mu^2 \beta_z^2)^2 + \mu^2 \beta_z^2}$$

$$= \left(\frac{j_x}{\epsilon_0} \right) \frac{1}{(1 - \mu^2 \beta_z^2) + \frac{\mu^2 \beta_z^2}{1 - \mu^2 \beta_z^2}}$$

$$= \left(\frac{j_x}{\epsilon_0} \right) \frac{1}{1 - \mu^2 \beta_z^2 + \mu^4 \beta_z^2 (1 + \mu^2 \beta_z^2)}$$

$$= \left(\frac{j_x}{\epsilon_0} \right) \frac{1}{1 + (\mu^2 \beta_z^2)^2} \approx \left(\frac{j_x}{\epsilon_0} \right)$$

4th order in β_z

Numbers: $\frac{j_x}{\epsilon_0} = \frac{I_x}{L} R_0 \left(= \frac{I_x}{Wd} \frac{R_0 Wd}{L} \right)$

$$= 200 \frac{V}{cm}$$

$$\rightarrow \underline{V_x} = - \bar{E}_x L = \underline{-200V}$$

$$\underline{V_y} = - \bar{E}_y W = \frac{j_x}{\epsilon_0} \mu \beta_z W = \underline{3.2V}$$