

Solutions:

$$(a) F_n(0) = kT \ln \left(\frac{G_L \tau_n}{n_i} \right) = 0.0259 \text{ eV} \ln \left(\frac{10^{12}}{10^{10}} \right) = \boxed{0.12 \text{ eV}}$$

→ low level injection

$$F_p(0) = -kT \ln \left(\frac{NA}{n_i} \right) = -0.0259 \text{ eV} \ln \left(\frac{10^{16}}{10^{10}} \right) = \boxed{-0.36 \text{ eV}}$$

$$(b) I_n(0) = -A n(0) \mu_n \frac{dF_n}{dx} = (10^{-2} \text{ cm}^2) (10^{12} \text{ cm}^{-3}) (714 \text{ cm}^2/\text{Vs}) \left(\frac{0.36 + 0.12 \text{ eV}}{8 \times 10^{-4} \text{ cm}} \right) \cdot \left(\frac{1.6 \times 10^{-19} \text{ C}}{e} \right) \text{ A}$$
$$= \boxed{0.685 \text{ mA}}$$

$$(c) n(x) \approx n(0) e^{-x/L_n} = n_i e^{\frac{F_n(x) - E_i}{kT}} = n_i e^{\frac{F_n(0) - Ax - E_i}{kT}}, \quad A = \frac{0.06 \text{ eV}}{\mu\text{m}}$$

$$\cancel{n(0)} e^{-x/L_n} = \cancel{n_i} e^{\frac{F_n(0) - E_i}{kT}} \cdot e^{-\frac{Ax}{kT}}$$

$$x/L_n = Ax/kT \quad \rightarrow \quad L_n = \frac{kT}{A} = \frac{0.0259 \text{ eV}}{0.06 \text{ eV}} \mu\text{m}$$

$$L_n = 0.43 \mu\text{m}; \quad D_n = L_n^2 / \tau_n = \boxed{18.5 \text{ cm}^2/\text{s}}$$

$$(d) I_{\text{total}} = 2 \cdot 0.685 \text{ mA} = 1.37 \text{ mA}, \text{ therefore } I_p(8 \mu\text{m}) \approx 1.37 \text{ mA}$$

$$I_p(8 \mu\text{m}) = A_p(8 \mu\text{m}) \mu_p \frac{dF_p}{dx} = (10^{-2} \text{ cm}^2) (10^{16} \text{ cm}^{-3}) (357 \text{ cm}^2/\text{Vs}) \frac{dF_p}{dx} \cdot \left(\frac{1.6 \times 10^{-19} \text{ C}}{e} \right) = 1.37 \times 10^{-3} \text{ A}$$

$$\frac{dF_p}{dx} = \frac{(1.37 \times 10^{-3})}{(1.6 \times 10^{-19}) (10^{-2}) (10^{16}) (357)} \cdot \frac{\text{eV}}{\text{cm}} = 0.240 \text{ eV/cm}, \quad \text{XXXXXXXXXX}$$

$$\boxed{2.4 \times 10^{-5} \text{ eV}/\mu\text{m}}$$