

Sparsity-Promoting Optimal Wide-Area Control of Power Networks

Florian Dörfler, *Member, IEEE*, Mihailo R. Jovanović, *Senior Member, IEEE*, Michael Chertkov, *Member, IEEE*, and Francesco Bullo, *Fellow, IEEE*

Abstract—Inter-area oscillations in bulk power systems are typically poorly controllable by means of local decentralized control. Recent research efforts have been aimed at developing wide-area control strategies that involve communication of remote signals. In conventional wide-area control, the control structure is fixed *a priori* typically based on modal criteria. In contrast, here we employ the recently-introduced paradigm of sparsity-promoting optimal control to simultaneously identify the optimal control structure and optimize the closed-loop performance. To induce a sparse control architecture, we regularize the standard quadratic performance index with an ℓ_1 -penalty on the feedback matrix. The quadratic objective functions are inspired by the classic slow coherency theory and are aimed at imitating homogeneous networks without inter-area oscillations. We use the New England power grid model to demonstrate that the proposed combination of the sparsity-promoting control design with the slow coherency objectives performs almost as well as the optimal centralized control while only making use of a single wide-area communication link. In addition to this nominal performance, we also demonstrate that our control strategy yields favorable robustness margins and that it can be used to identify a sparse control architecture for control design via alternative means.

Index Terms—Alternating direction method of multipliers, inter-area modes, sparsity-promoting control, wide-area control.

I. INTRODUCTION

BULK power systems typically exhibit multiple electro-mechanical oscillations. *Local oscillations* are characterized by single generators swinging relative to the rest of the network, whereas *inter-area oscillations* are associated with the dynamics of power transfers and involve groups of generators

oscillating relative to each other. With steadily growing demand, deployment of renewables in remote areas, and deregulation of energy markets, long-distance power transfers outpace the addition of new transmission facilities. These developments lead to a maximum use of the existing network, result in smaller stability margins, and cause inter-area modes to be ever more lightly damped. In a heavily stressed grid, poorly damped inter-area modes can even become unstable. For example, the blackout of August 10, 1996, resulted from an instability of the 0.25 Hz mode in the Western interconnected system [2].

Local oscillations are typically damped by generator excitation control via power system stabilizers (PSSs) [3]. However, these *decentralized* control actions can interact in an adverse way and destabilize the overall system [4]. Sometimes inter-area modes cannot be even stabilized by PSSs [5], unless sufficiently many and carefully tuned PSSs are deployed [6]–[8]. Regarding tuning of conventional PSSs, high-gain feedback is necessary in some networks [5] but may destabilize other networks [6], [7]. Furthermore, even when decentralized controllers provide stability they may result in poor performance, and their optimal tuning presents non-trivial design challenges.

In principle, the above problems can be solved by distributed *wide-area control* (WAC), where controllers make use of remote measurements and control signals. WAC is nowadays feasible thanks to recent technological advances including fast and reliable communication networks, high-bandwidth and time-stamped phasor measurement units (PMUs), and flexible AC transmission system (FACTS) devices. We refer to the surveys [9]–[11] and the articles in [12] for a detailed account of technological advances and capabilities. Several efforts have been directed towards WAC of oscillations based on robust and optimal control methods; see [12]–[19] and references therein. The chosen performance metrics include frequency domain and root-locus criteria, signal amplifications from disturbance inputs to tie line flows, inter-area angles, or machine speeds.

In comparison to local control, WAC involves the communication of remote signals and may suffer from additional vulnerabilities, such as uncertain communication channels, time delays, and the lack of globally known models and their time constants. Known time delays can be incorporated into the control design, for example, via linear matrix inequalities [6], [17] or predictor-based design [19]. Unknown time constants can be treated using linear parameter-varying systems [13] or online identification of parameters [16], aggregated models [20], or non-parameterized models [21]–[23]. Unknown delays, communication uncertainties, and uncertain time constants can be incorporated into a robust control synthesis using (un)structured uncertainties and robustness margins [24].

Manuscript received July 11, 2013; revised November 11, 2013; accepted January 27, 2014. Date of publication February 13, 2014; date of current version August 15, 2014. This material is based in part upon work supported by the NSF grants IIS-0904501, CPS-1135819, and CMMI-09-27720. A preliminary and abbreviated version of this document has been presented in [1]. Paper no. TPWRS-00900-2013.

F. Dörfler is with the Electrical Engineering Department, University of California Los Angeles, Los Angeles, CA 90095 USA (e-mail: dorfler@seas.ucla.edu).

M. R. Jovanović is with the Department of Electrical and Computer Engineering, University of Minnesota, Minneapolis, MN 55455 USA (e-mail: mihailo@umn.edu).

M. Chertkov is with Theory Division & Center for Nonlinear Studies at LANL and with New Mexico Consortium, Los Alamos, NM 87544 USA (e-mail: chertkov@lanl.gov).

F. Bullo is with the Department of Mechanical Engineering, University of California Santa Barbara, Santa Barbara, CA 93106 USA (e-mail: bullo@engineering.ucsb.edu).

Color versions of one or more of the figures in this paper are available online at <http://ieeexplore.ieee.org>.

Digital Object Identifier 10.1109/TPWRS.2014.2304465

Typically, the controllers are designed for pre-specified sensor and actuator locations and an *a priori* fixed sparsity pattern that induces the necessary communication structure. In an attempt to identify optimal sensor or actuator placements and to reduce the communication complexity and the interaction between control loops, different strategies aim at identifying few but critical control channels [18], [25]–[28]; see [11] and [29] for a comparison and robustness evaluation. These strategies rely on modal perspectives and aim at maximizing geometric metrics such as modal controllability and observability residues. As a result, the control channels are typically chosen through combinatorial SISO criteria and not in an optimal way.

Another body of literature relevant to our study is optimal control subject to structural constraints, for example, a desired sparsity pattern of the feedback matrix in static state feedback design [30]. In general, control design subject to structural constraints is hard, stabilizability is not guaranteed, and optimal control formulations are not convex for arbitrary structural constraints [31]. Furthermore, in the absence of pre-specified structural constraints, most optimal control formulations result in controllers without any sparsity structure according to which measurements and control channels can be selected, and they typically require a centralized implementation. In order to overcome these limitations of decentralized optimal control, alternative strategies have recently been proposed that simultaneously identify the control structure and optimize the closed-loop performance; see [32]–[37]. The proposed strategies combine classic optimal and robust control formulations with recent advances in compressed sensing [38].

Here we investigate a novel approach to WAC design for bulk power systems. We follow the sparsity-promoting optimal control approach developed in [37] and find a linear static state feedback that simultaneously optimizes a standard quadratic cost criterion and induces a sparse control structure. Our choice of performance criterion is inspired by the classic work [39]–[41] on slow coherency. We propose a novel criterion that encourages the closed-loop system to imitate a homogeneous network of identical generators with no inter-area oscillations. Besides this physical insight, an additional advantage of our performance criteria is that the optimal controller makes use of readily accessible state variables such as angles and frequencies. In the performance and robustness assessment of our sparsity-promoting optimal control synthesis, we emphasize robustness to time delays, gain uncertainties, and variable operating conditions arising in WAC implementation.

We consider a coordinated PSS design for the IEEE 39 New England power grid model to illustrate the utility of our approach. This compelling example shows that, with only a single WAC link, it is possible to achieve nearly the same performance as a centralized optimal controller. In particular, our sparsity-promoting controller is within 1.5882% of the performance achieved by the optimal centralized controller. Besides this nominal performance level, we also show that the identified control structure is not sensitive to the chosen operating point, and that robustness margins gracefully deteriorate as the control structure becomes increasingly sparse. We also illustrate the robustness of our WAC strategy through simulations with communication noise and delays. Finally,

we show that our approach can also be used to identify a sparse architecture for control design via alternative means. In particular, we use nonlinear simulations to demonstrate that the closed-loop performance can be significantly improved with a proportional feedback of a single remote measurement (identified by our sparsity-promoting framework).

The remainder of the paper is organized as follows: Section II describes the sparsity-promoting optimal control approach with the slow coherency objectives. Section III shows the application to the New England Power Grid. The algorithmic implementation and a link to our source code can be found in the Appendix. Finally, Section IV concludes the paper.

II. PROBLEM SETUP AND THEORETICAL FRAMEWORK

A. Modeling of Generation, Transmission, and Control

We initially consider a detailed, nonlinear, and differential-algebraic power network model of the form

$$\dot{x}(t) = f(x(t), z(t), u(t), \eta(t)) \quad (1a)$$

$$0 = g(x(t), z(t), u(t), \eta(t)) \quad (1b)$$

where the dynamic and algebraic variables $x(t) \in \mathbb{R}^n$ and $z(t) \in \mathbb{R}^s$ constitute the state, $u(t) \in \mathbb{R}^p$ is the control action, and $\eta(t) \in \mathbb{R}^q$ is a white noise signal. Here, the dynamic equations (1a) account for the electromechanical dynamics of synchronous generators and their excitation control equipment. The algebraic equations (1b) account for load flow, generator stator, and power electronic circuit equations. The control input $u(t) \in \mathbb{R}^p$ enters through either power electronics (FACTS), generator excitation (PSS) or governor control. Finally, the noise can arise from disturbances in the control loops, or fluctuating loads and generator mechanical power inputs. Though not explicitly considered in this article, the differential-algebraic model (1) and our analysis are sufficiently general to allow for dynamic loads, synchronous condensers, and detailed models of FACTS devices.

Next we linearize the system (1) at a stationary operating point, solve the resulting linear algebraic equations for the variable $z(t)$, and arrive at the linear state-space model

$$\dot{x}(t) = Ax(t) + B_1\eta(t) + B_2u(t) \quad (2)$$

where $A \in \mathbb{R}^{n \times n}$, $B_1 \in \mathbb{R}^{n \times q}$, and $B_2 \in \mathbb{R}^{n \times p}$. The linear model (2) is of large scale and its time constants depend on the current operating point. Thus, the precise model (2) of a bulk power system may not be known system-wide, or it may be known only with a limited accuracy. We discuss related robustness issues in Section II-F. As discussed in Section I, the model (2) can also be estimated online using subspace identification methods [21]–[23], identification of aggregated models [20], or adaptive Kalman filtering methods [16].

B. Review of Slow Coherency Theory

To obtain an insightful perspective on inter-area oscillations, we briefly recall the classic slow coherency theory [39]–[41]. Let the state variable x of the power network model (1) [or its linearization (2)] be partitioned as $x = [\theta^T \ \dot{\theta}^T \ x_{\text{rem}}^T]^T$, where

$\theta, \dot{\theta} \in \mathbb{R}^{n_g}$ are the rotor angles and frequencies of n_g synchronous generators and $x_{\text{rem}} \in \mathbb{R}^{n-2n_g}$ are the remaining state variables, which typically correspond to fast electrical dynamics. In the absence of higher-order generator dynamics, and for constant-current and constant-impedance loads, the power system dynamics (1) can be reduced to the electromechanical swing dynamics of the generators [3]:

$$M_i \ddot{\theta}_i + D_i \dot{\theta}_i = P_{\text{red},i} - \sum_{j=1}^{n_g} |Y_{\text{red},ij}| E_i E_j \sin(\theta_i - \theta_j - \varphi_{ij}). \quad (3)$$

Here, M_i and D_i are the inertia and damping coefficients, E_i is the q -axis voltage, and $P_{\text{red},i}$ is the generator power injection in the network-reduced model. The Kron-reduced admittance matrix Y_{red} describes the interactions among the generators, and the phase shifts $\varphi_{ij} \triangleq -\arctan(\Re(Y_{\text{red},ij})/\Im(Y_{\text{red},ij})) \in [0, \pi/2[$ are due to transfer conductances $\Re(Y_{ij})$ [42]. When linearized at an operating point $(\theta^*, \dot{\theta}^*)$, the swing equation (3) read as

$$M\ddot{\theta} + D\dot{\theta} + L\theta = 0 \quad (4)$$

where M and D are the diagonal matrices of inertia and damping coefficients, and L is a Laplacian matrix with off-diagonals $L_{ij} = -|Y_{\text{red},ij}| E_i E_j \cos(\theta_i^* - \theta_j^* - \varphi_{ij})$ and diagonal elements $L_{ii} = -\sum_{j=1, j \neq i}^{n_g} L_{ij}$. Notice that, in the absence of transfer conductances, equation (4) describes a dissipative mechanical system with kinetic energy $(1/2) \cdot \dot{\theta}^T M \dot{\theta}$ and potential energy $(1/2) \cdot \theta^T L \theta$. Since M and D are diagonal, the interactions among generators in (4) are entirely described by the weighted graph induced by the Laplacian matrix L .

Inter-area oscillations may arise from non-uniform inertia and damping coefficients (resulting in slow and fast responses), clustered groups of machines (swinging coherently) and sparse interconnections among them, as well as large inter-area power transfers.¹ Assume that the set of generators $\mathcal{V} = \{1, \dots, n_g\}$ is partitioned in multiple coherent (and disjoint) groups of machines (or areas), that is, $\mathcal{V} = \mathcal{V}_\alpha \cup \mathcal{V}_\beta \cup \dots$. Then it can be shown [39]–[41] that the long-time dynamics of each area α with nodal set \mathcal{V}_α are captured by the aggregate variable $\delta_\alpha = (\sum_{i \in \mathcal{V}_\alpha} M_i \theta_i) / (\sum_{i \in \mathcal{V}_\alpha} M_i)$ describing the center of mass of area α . The slow inter-area dynamics are obtained as

$$\tilde{M}\ddot{\delta} + \tilde{D}\dot{\delta} + \tilde{L}\delta = 0 \quad (5)$$

where $\delta = [\delta_\alpha \ \delta_\beta \ \dots]^T$ and \tilde{M} , \tilde{D} , and \tilde{L} are the aggregated inertia, dissipation, and Laplacian matrices.

C. Local and Wide-Area Control Design

As illustrated in the block diagram² in Fig. 1, we seek for linear time-invariant control laws and follow a two-level control strategy of the form $u(t) = u_{\text{loc}}(t) + u_{\text{wac}}(t)$.

In the first step, the local control $u_{\text{loc}}(t)$ is designed based on locally available measurements and with the objective of sta-

¹A large power transfer between two nodes i, j in distinct areas amounts to a large steady state difference angle $|\theta_i^* - \theta_j^*|$. Equivalently, in the linearized model (4), the coupling $|L_{ij}| = |Y_{\text{red},ij}| E_i E_j \cos(\theta_i^* - \theta_j^* - \varphi_{ij})$ is small.

²In Fig. 1, the system dynamics (A matrix) includes the power network dynamics and the local control loops. The WAC signal is added to the PSS input. Alternatively, the WAC signal can be added to the automatic voltage regulator (AVR). Both strategies have been advocated, see [6], [17], [18].

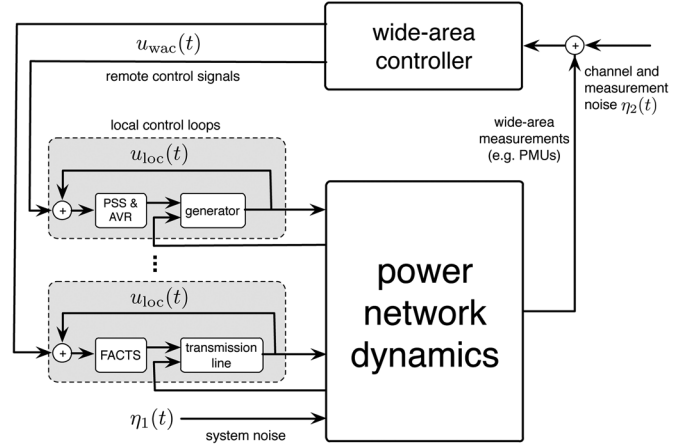


Fig. 1. Two-level control design combining local and wide-area control.

bilizing each isolated component. For example, $u_{\text{loc}}(t)$ can be obtained by a conventional PSS design with the objective of suppressing local oscillations [3]. Next, the wide-area control $u_{\text{wac}}(t)$ is designed to enhance the global system behavior and suppress inter-area oscillations. For this second design step, the local control $u_{\text{loc}}(t)$ is assumed to be absorbed into the plant (2). Additionally, since $u_{\text{wac}}(t)$ relies on the communication of remote signals, the two-level control strategy guarantees a nominal performance level in case of communication failures.

D. Sparsity-Promoting Linear Quadratic Control

As discussed in Section I, an inherent problem in WAC is the proper choice of *control architecture*, that specifies which quantities need to be measured and which controller needs to access which measurement. Here, we confine our attention to static state feedback $u_{\text{wac}}(t) = -Kx(t)$, where the control structure is determined by the sparsity pattern of the feedback gain $K \in \mathbb{R}^{p \times n}$. We use the sparsity-promoting optimal control framework [37] to minimize the ℓ_1 -regularized steady-state variance of a stochastically-driven closed-loop system:

$$\begin{aligned} \text{minimize} \quad & \lim_{t \rightarrow \infty} \mathcal{E} \{ x(t)^T Q x(t) + u(t)^T R u(t) \} \\ & + \gamma \sum_{i,j} w_{ij} |K_{ij}| \end{aligned}$$

subject to

$$\text{dynamics : } \dot{x}(t) = Ax(t) + B_2 u(t) + B_1 \eta(t)$$

$$\text{linear control : } u(t) = -Kx(t)$$

$$\text{stability : } (A - B_2 K) \text{ Hurwitz.} \quad (6)$$

Here, $\gamma \geq 0$ is a nonnegative parameter, $\mathcal{E}\{\cdot\}$ is the expectation operator, and $Q \in \mathbb{R}^{n \times n}$, $R \in \mathbb{R}^{p \times p}$ are positive semidefinite and positive definite matrices that denote the state and control weights, respectively. We assume that the triple $(A, B_2, Q^{1/2})$ is stabilizable and detectable. The term $\sum_{i,j} w_{ij} |K_{ij}|$ is a *weighted ℓ_1 -norm* of K , where $w_{ij} > 0$ are positive weights. The weighted ℓ_1 -norm serves as a proxy for the (non-convex) cardinality function $\text{card}(K)$ denoting the number of non-zero entries in K . An effective method for enhancing sparsity is to solve a sequence of weighted ℓ_1 -optimization problems, where the weights are determined by the solution of the weighted ℓ_1 -problem in the previous iteration; see [43] for further details.

An equivalent formulation of the optimal control problem (6) is given via the closed-loop observability Gramian P as

$$\begin{aligned} & \text{minimize} \quad J_\gamma(K) \triangleq \text{trace}(B_1^T P B_1) + \gamma \sum_{i,j} w_{ij} |K_{ij}| \\ & \text{subject to} \quad (A - B_2 K)^T P + P(A - B_2 K) \\ & \quad \quad \quad = -(Q + K^T R K). \end{aligned} \quad (7)$$

The latter formulation (7) is amenable to an iterative solution strategy using the alternating direction method of multipliers (ADMM); see [36] and [37]. The cost function in (7) is a linear combination of the \mathcal{H}_2 -norm of the closed-loop system

$$\begin{aligned} \dot{x}(t) &= (A - B_2 K)x(t) + B_1 \eta(t) \\ y(t) &= \begin{bmatrix} Q^{\frac{1}{2}} \\ -R^{\frac{1}{2}} K \end{bmatrix} x(t) \end{aligned}$$

and the sparsity-promoting term $\gamma \sum_{i,j} w_{ij} |K_{ij}|$. In what follows, for a fixed value of $\gamma \geq 0$, we denote the minimizer to (7) by K_γ^* and the optimal cost by $J_\gamma^* = J(K_\gamma^*)$. For $\gamma = 0$ the problem (7) reduces to the standard state-feedback \mathcal{H}_2 -problem [24] with the optimal gain K_0^* and the optimal cost J_0^* . On the other hand, for $\gamma > 0$ the weighted ℓ_1 -norm promotes sparsity in the feedback gain K_γ^* , thereby identifying essential pairs of control inputs and measured outputs.

To solve the sparsity-promoting optimal control problem (7), we rely on the approach proposed in [37] using ADMM. See the Appendix for details on the algorithmic implementation.

E. Choice of Optimization Objectives

The design parameters Q, R, B_1, γ need to be chosen with the objective of damping inter-area oscillations. The resulting feedback $u_{\text{vac}}(t)$, the control variables $K_\gamma^* x(t)$, the communication structure (the sparsity pattern of the off-diagonals of K_γ^*), and the control effort depend solely on the system model and our choices of the design parameters Q, R, B_1 , and γ .

State Cost: Slow coherency theory shows that an *ideal* power system without inter-area oscillations is characterized by uniform inertia coefficients and homogenous power transfers among generators. Equivalently, the Laplacian and inertia matrices in the linearized swing equation (4) take the form

$$L = L_{\text{unif}} = \ell \cdot \left(I_{n_g} - \left(\frac{1}{n_g} \right) \mathbb{1}_{n_g} \mathbb{1}_{n_g}^T \right), \quad M = M_{\text{unif}} = m \cdot I_{n_g}$$

where $\ell, m > 0$ are constants, I_{n_g} is the n_g -dimensional identity matrix, and $\mathbb{1}_{n_g}$ is the n_g -dimensional vector of ones.

Inspired by the above considerations, we choose the following performance specifications for the state cost:

$$x^T Q x = \frac{1}{2} \theta^T L_{\text{unif}} \theta + \frac{1}{2} \dot{\theta}^T M_{\text{unif}} \dot{\theta} + \varepsilon \cdot \|\theta\|_2^2 \quad (8)$$

where $\varepsilon \geq 0$ is a small regularization parameter. For $\varepsilon = 0$, the state cost $x^T Q x$ quantifies the kinetic and potential energy of a homogenous network composed of identical generators, and it penalizes frequency violations and angular differences. The cost $x^T Q x$ does not penalize deviations in the generator voltages,

the states of the excitation system, or the local control $u_{\text{loc}}(t)$ included in the A matrix. The regularization term $\varepsilon \|\theta\|_2^2$ assures numerical stability and detectability³ of $(A, Q^{1/2})$.

As we will see in Section III, the state cost (8) results in an improved *average* closed-loop performance with all inter-area modes either damped or distorted. If the objective is to reject a *specific* inter-area mode, for example, a dominant inter-area mode featuring the two groups \mathcal{V}_α and \mathcal{V}_β , then the discussion preceding the inter-area dynamics (5) suggests the cost

$$x^T Q x = \ell \cdot \|\delta_\alpha - \delta_\beta\|_2^2 + m \cdot \|\dot{\delta}_\alpha - \dot{\delta}_\beta\|_2^2 + \varepsilon \cdot \|\theta\|_2^2 \quad (9)$$

where $\ell, m > 0$ are gains, $\delta_\alpha, \delta_\beta$ are the aggregate variables, and $\varepsilon \geq 0$ is a small regularization parameter.

Alternative cost functions penalize selected generator frequency deviations or branch power flows $|L_{ij}|(\theta_i - \theta_j)$ to assure coherency and guarantee (soft) thermal limit constraints. Finally, linear combinations of all cost functions can also be chosen.

In the costs (8) and (9), the parameter m mainly affects the frequency damping, whereas the parameter ℓ affects the damping of the machine difference angles, that is, inter-area power flows. In summary, the state costs (8)–(9) reflect the insights of slow coherency theory, and, as we will see later, they also promote the use of readily available control variables.

Control Cost: For simplicity and in order to minimize interactions among generators the control effort is penalized as $u^T R u$, where R is a positive definite diagonal matrix. Larger diagonal values of R result in a smaller control effort.

System Noise: In standard (centralized) linear quadratic control, the optimal feedback gain K_0^* is independent of the choice of B_1 [24]. However, for $\gamma > 0$ the optimal feedback gain K_γ^* depends on the choice of B_1 ; see the necessary optimality conditions in [37]. In order to mitigate the impacts of noisy or lossy communication among spatially distributed controllers, one may choose $B_1 = B_2$. Otherwise, B_1 can be chosen to include load and generation uncertainties in (1).

Promoting Sparsity: For $\gamma = 0$, the optimal control problem (7) reduces to a standard state-feedback \mathcal{H}_2 -problem whose solution can be obtained from the positive definite solution to the algebraic Riccati equation. Starting from this initial value, we iteratively solve the optimal control problem (7) for increasingly larger values of γ . We found that a logarithmically spaced sequence of γ -values performs well in practice. In the end, the resulting sequence of optimal controllers is analyzed, and a value of γ is chosen to strike a balance between the closed-loop performance and sparsity of the controller.

In summary, if the state costs (8) or (9) are chosen, then the parameters affecting the optimal feedback gains K_γ^* are $\ell, m, \varepsilon, B_1$, the diagonal values of R , and the sequence of γ -values.

³If the power system model (1) entails a slack bus, then ε can be set to zero. Otherwise, there is a marginally stable and unobservable mode corresponding to the rotational symmetry of the power flow: a uniform shift of all angles does not change the vector field (1). The optimal control problem (7) is still feasible, and the marginally stable mode is not affected by controllers using only angular differences (i.e., power flows) [37], [44]. To guarantee a simple numerical treatment of the resulting Riccati equations using standard software, an inclusion of a small positive regularization parameter $\varepsilon > 0$ is necessary.

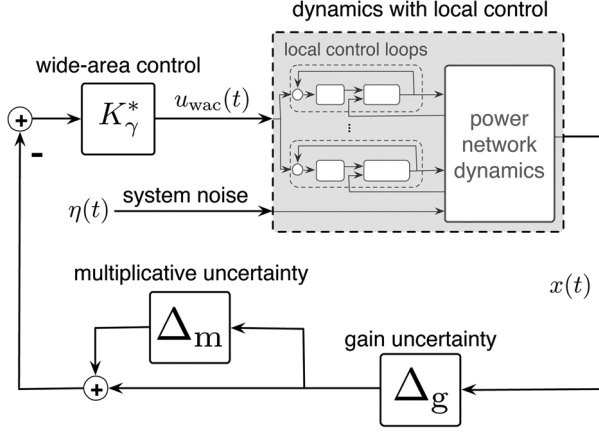


Fig. 2. Gain uncertainties Δ_g and multiplicative uncertainties Δ_m account for delays and uncertain (or unmodeled) dynamics in the WAC channel.

F. Robustness, Time Delays, and Gain Uncertainties

As discussed in Section I, WAC may have to deal with uncertain communication channels, time delays, and the lack of precisely known system-wide time constants. In particular, time delays may arise from communication delays, latencies and multiple data rates in the SCADA (supervisory control and data acquisition) network, asynchronous measurements, and local processing and operating times. As a result, local control signals and measurements may have different rates and time stamps than WAC signals obtained from remote sites.

Given the above vulnerabilities, the wide-area control loop needs to be robust to gain uncertainties Δ_g and multiplicative uncertainties Δ_m , as depicted in Fig. 2. For instance, if the channel from measurement i to control input j features a time-delay, then the (i, j) th entry of Δ_g is a pure phase delay. We refer to [24, Section 7.4] for the modeling of delays with multiplicative uncertainties Δ_m . In a general robust control theory framework, the uncertainty blocks Δ_g and Δ_m are unknown, stable, and proper dynamical systems that typically satisfy certain norm bounds on their input-output behavior.

Standard frequency domain arguments show that robustness to delays is directly related to phase margins [24]. For a non-interacting (i.e., diagonal) uncertainty Δ_g , the optimal centralized feedback gain K_0^* results in guaranteed phase margins of $\pm 60^\circ$, lower gain (reduction) margins of 0.5, and upper gain (amplification) margins of ∞ in every channel [45]. For an unstructured multiplicative uncertainty Δ_m , the optimal centralized feedback gain K_0^* guarantees closed-loop stability provided that its \mathcal{L}_2 -induced input-output norm is bounded by 0.5 corresponding to a multivariable phase margin of 30° [46].

Yet another source of uncertainty results from the fact that the time constants of the linearized model (2) depend on the current operating condition of the overall power system. The gain margins discussed in preceding paragraphs provide safeguards against gain uncertainties in the control loop arising, for example, from variable or uncertain time constants in the generator excitation system or the measurement channels.

For the γ -parameterized family of sparsity-promoting controllers, we explicitly verify robustness to phase and gain uncertainties in Section III. In particular, we observe that the phase and gain margins decay gracefully for K_γ^* as γ increases. Alternatively, robustness to *known* time delays can be included in the

TABLE I
INTER-AREA MODES OF NEW ENGLAND POWER GRID WITH PSSs

mode no.	eigenvalue pair	damping ratio	frequency [Hz]	coherent groups
1	$-0.6347 \pm i 3.7672$	0.16614	0.59956	10 vs. all others
2	$-0.7738 \pm i 6.7684$	0.11358	1.0772	1,8 vs. 2-7,9,10
3	$-1.1310 \pm i 5.7304$	0.19364	0.91202	1,2,3,8,9 vs. 4-7
4	$-1.1467 \pm i 5.9095$	0.19049	0.94052	4,5,6,7,9 vs. 2,3
5	$-1.5219 \pm i 5.8923$	0.25009	0.93778	4,5 vs. 6,7

control design by explicitly accounting for delays via Padé approximations (absorbed in the plant) [24].

III. COORDINATED SUPPLEMENTARY PSSs DESIGN

In this section, we use the IEEE 39 New England power grid model to validate performance of the proposed WAC strategy. This model consists of 39 buses and 10 two-axis generator models, where generator 10 is an equivalent aggregated model.

A. Local Control Design and Inter-Area Dynamics

The *Power System Toolbox* [47] was used to obtain the non-linear differential-algebraic model (1) and the linear state space system (2). The open-loop system is unstable, and the generators are equipped with PSS excitation controllers designed with washout filters and lead/lag elements. For generator i , the local PSS reads in the Laplace domain as

$$u_{loc,i}(s) = k_i \cdot \frac{T_{w,i}s}{1 + T_{w,i}s} \cdot \frac{1 + T_{n1,i}s}{1 + T_{d1,i}s} \cdot \frac{1 + T_{n2,i}s}{1 + T_{d2,i}s} \cdot \dot{\theta}_i(s) \quad (10)$$

where, with an abuse of notation, $\dot{\theta}_i(s)$ and $u_{loc,i}(s)$ denote the Laplace transforms of $\dot{\theta}_i(t)$ and $u_{loc,i}(t)$, respectively. The controller gains are chosen according to the tuning strategy [8] as $T_{w,i} = 3$, $T_{n1,i} = T_{n2,i} = 0.1$, $T_{d1,i} = T_{d2,i} = 0.01$ for $i \in \{1 \dots 9\}$, $k_i = 12$ for $i \in \{1, 2, 3, 5, 6, 9\}$, $k_4 = 10$, $k_7 = 11.03$, and $k_8 = 9.51$. As in [8], we adopt the first-order exciter model, and choose uniform time constants $T_a = 0.015$ s and regulator gains $K_a = 200$ for all generators. The static DC gains $K_a \cdot k_i$ in the exciter and PSS control channels are slightly different compared to the highly tuned data in [8]. We made this choice for the sake of illustration: the PSSs (10) provide good damping for the local modes and stabilize the otherwise unstable open-loop system (2). On the other hand, the chosen PSSs do not severely distort the shapes of the inter-area modes unless they are very carefully tuned to the linearized model (depending on the particular operating condition).

An analysis of the closed-loop modes and participation factors reveals the presence of five dominant inter-area modes. These five modes are reported in Table I, and the groups of coherent machines and the frequency components of the associated eigenvectors are illustrated in Fig. 3.

B. WAC Design and Nominal Performance

To provide additional damping for the inter-area oscillations, we design a supplementary WAC signal $u_{wac}(t)$ which additively enters the AVRs of the controlled generators. The sparsity-promoting optimal control strategy (6) is used to design $u_{wac}(t)$, where the state cost (8) is selected with $\varepsilon = 0.1$ and $(\ell, m) = (2, 2)$. To share the control burden equally we set the control weight to be identity $R = I$. This choice results in a WAC signal $u_{wac}(t)$ of the

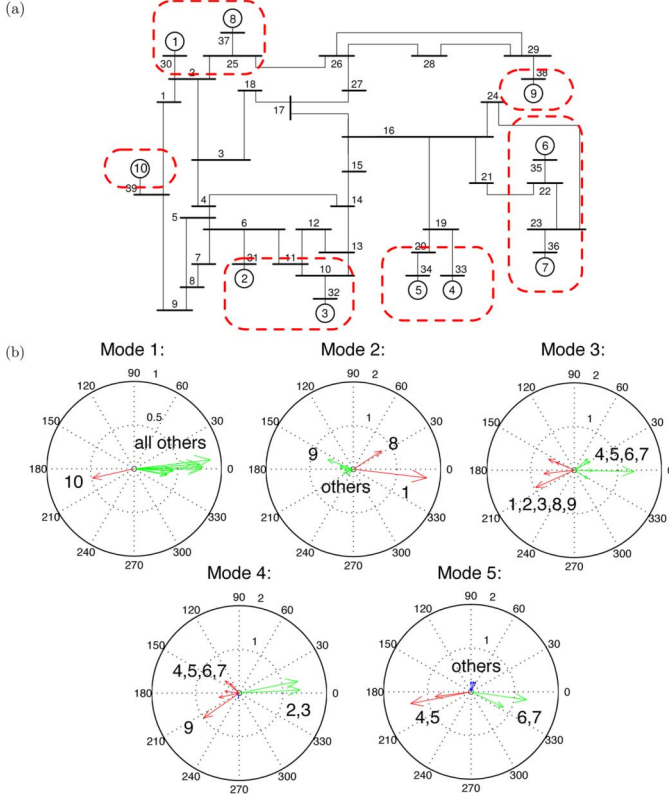


Fig. 3. Subfigure (a) displays the IEEE 39 New England power grid and its coherent groups. The polar plots in Subfigure (b) show the generator frequency components of the five dominant inter-area modes.

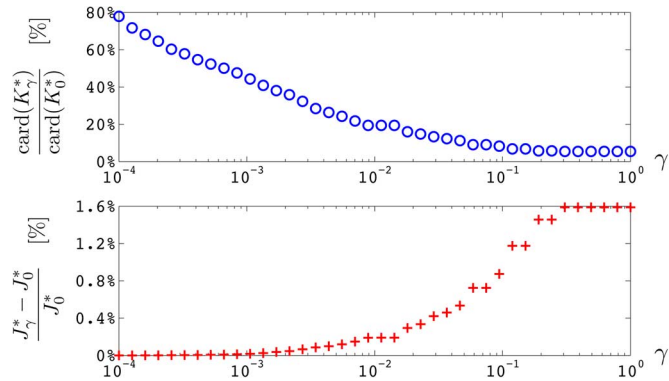


Fig. 4. Number of nonzero entries in the sparse feedback gain K_γ^* and the performance degradation of K_γ^* relative to the optimal centralized gain K_0^* .

same magnitude as the local control signal $u_{loc}(t)$, that is, $\max_{t \in \mathbb{R}_{\geq 0}} \|u_{wac}(t)\|_\infty \approx \max_{t \in \mathbb{R}_{\geq 0}} \|u_{loc}(t)\|_\infty$, and it avoids input saturation. Furthermore, to reject communication noise in the WAC implementation, we choose $B_1 = B_2$. Finally, we solve the optimal control problem (7) for 40 logarithmically spaced values of γ in the interval $[10^{-4}, 10^0]$. Our results are reported in Figs. 4 and 5.

For $\gamma = 0$, the optimal feedback gain K_0^* is fully populated, thereby requiring centralized implementation. As γ increases, the off-diagonal elements of the feedback matrix K_γ^* become significantly sparser whereas the relative cost $(J_\gamma^* - J_0^*)/J_0^*$ increases only slightly; see Figs. 4 and 5. Additionally, as γ increases, the state cost (8) promotes the use of angles and speeds

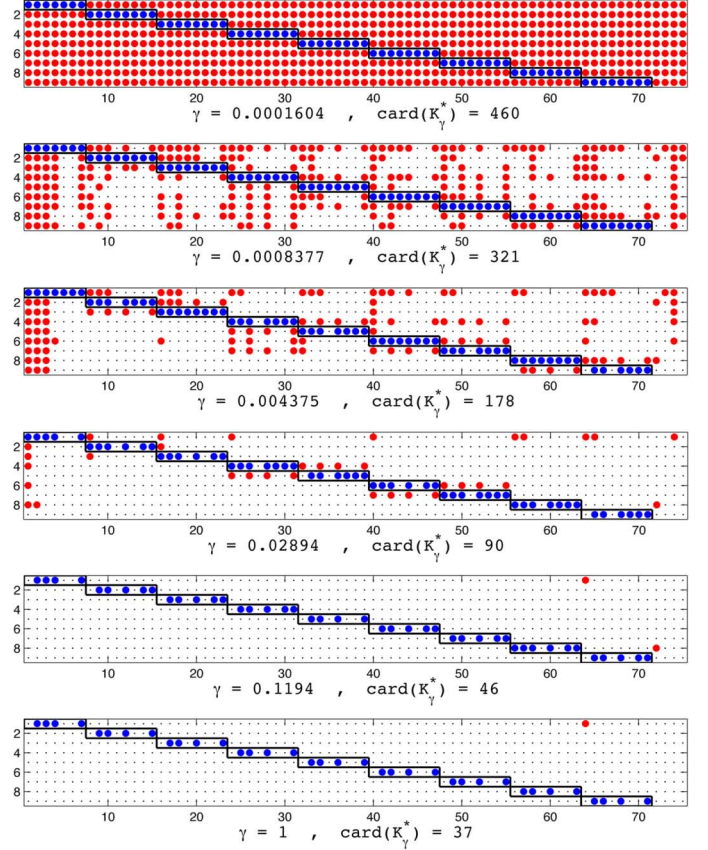


Fig. 5. The sparsity patterns of K_γ^* illustrate the control architecture. A nonzero (i, j) element of K_γ^* (denoted by a colored dot) implies that controller i needs to access state j . The diagonal blocks (framed) with blue dots correspond to local feedback, and the off-diagonal blocks with red dots correspond to remote feedback signals. As γ increases, the information exchange becomes sparser, and angles and frequencies (the first two states of each vertical block) become the sole signals to be communicated.

in the off-diagonal elements of K_γ^* , and most nonzero elements of K_γ^* correspond to local feedback. For $\gamma = 1$, the optimal controller K_1^* is within 1.5882% of the optimal centralized performance even though only a single signal needs to be communicated: the controller at generator 1 needs to access $\theta_9(t)$. As expected, as γ increases most of the control burden is on generator 1, which has the largest inertia of all controlled generators. Likewise, the angle of loosely connected⁴ generator 9 needs to be measured and communicated to generator 1. The identified WAC channel $9 \rightarrow 1$ appears to be necessary to suppress the inter-area mode 2 in Table I, which is mainly dominated by generators 1 and 9.

Fig. 6 displays the spectrum of the open-loop matrix A and the closed-loop matrix $A - B_2 K_\gamma$ for different values of γ . We make the following observations: First, as γ increases, the locations of the poles of $A - B_2 K_\gamma$ do not change significantly, and the poorly damped poles essentially overlap. This confirms our observation from Fig. 4: K_γ (with $\gamma > 0$) achieves a similar performance as the centralized feedback gain K_0 . Second, the weakly damped pair of poles (with nearly zero imaginary part and very high damping ratio 0.7452) is an artifact of the ε -regularization in (8). For $\varepsilon \searrow 0$, this pole pair becomes real

⁴In terms of graph theory, the sum of effective resistances [42] between generator 9 and the others is very large compared to remaining network.

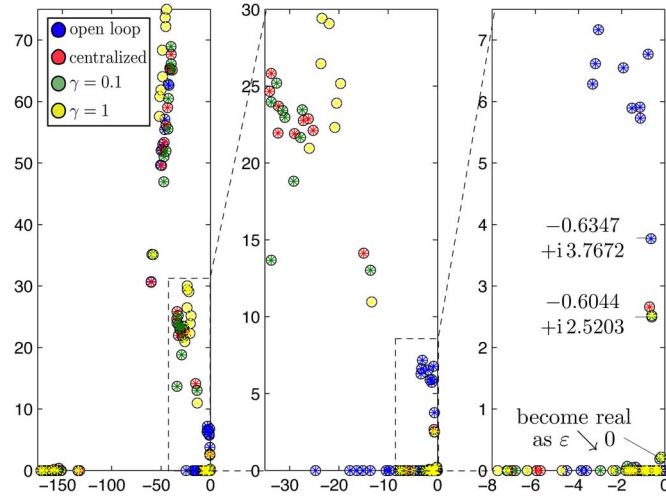


Fig. 6. Spectrum of the WAC open loop matrix A displayed in blue and the spectrum of the WAC closed-loop matrix $A - B_2 K_\gamma$ for $\gamma \in \{0, 0.1, 1\}$ displayed in red, green, and yellow, respectively. The central and right panels are magnifications of the left and central panel, respectively.

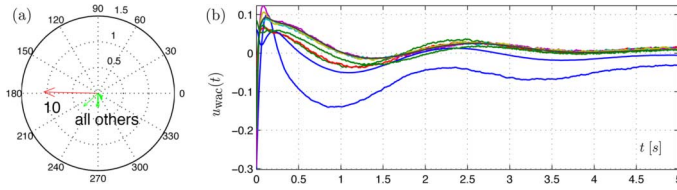


Fig. 7. Subfigure (a) displays the frequency components of the least damped oscillatory mode of the closed loop with local PSSs and WAC. Subfigure (b) shows the WAC signal $u_{\text{wac}}(t)$. The initial conditions are aligned with the eigenvector of the dominant open-loop inter-area mode 1, and $u_{\text{wac}}(t)$ is subject to additive white noise with zero mean and standard deviation 0.01.

and one of the poles becomes zero corresponding to the rotational symmetry of the power flow. Third, in comparison with the open loop, the wide-area controller does not significantly change the real part of the eigenvalues of the weakly damped oscillatory modes. Rather, the closed-loop performance is improved by increasing the damping ratio and distorting the associated eigenvectors. Apart from one pair of eigenvalues located at $-0.6044 \pm i2.5203$ with high damping ratio 0.239 (possibly corresponding to the inter-area mode 1 in Table I), all other complex-conjugate eigenvalue pairs are left of the asymptote $\text{Real}(s) = -12.74$. From the frequency components of its eigenvector [in Fig. 7(a)] and the frequency time series [in Fig. 8(a) and (b)], it can be seen that this mode does not anymore correspond to generators oscillating against each other. As a consequence, poorly damped power flow oscillations between the areas $\mathcal{V}_\alpha = \{1 \dots 9\}$ and $\mathcal{V}_\beta = \{10\}$ have been suppressed; see Fig. 8(d) and 8(e). We finally note that, besides the critical mode, the damping ratio is also significantly improved for all other weakly damped modes.

C. Implementation Issues, Robustness, and Delays

As discussed in Section II-F, multivariable phase margins are well suited robustness measures to account for communication delays, latencies in the SCADA network, and asynchronous measurements of generator rotor angles. Here, we investigate how the general multivariable phase margin of the WAC closed

loop changes with the sparsity-promoting parameter γ ; see Fig. 9. Similar to the performance and sparsity levels of K_γ^* in Fig. 4, the multivariable phase margin is nearly a monotonic function of $\gamma \in [10^{-4}, 10^0]$. Over the range of examined values of γ , the phase margin experiences a modest drop of about 4° . Similar observations can be made about the multivariable gain reduction and amplification margins displayed in Fig. 9. They deteriorate gracefully, in a monotonic way, and by comparatively small amounts. Hence, each PSS gain can differ from its nominal gain [used to construct the linearized model (2)] and independently from other PSS gains by a factor of order $[0.2, 5]$ even for $\gamma = 1$. We thus conclude that the controller resulting from the sparsity-promoting optimal control problem (6) enjoys nearly the same robustness properties as the optimal centralized controller.

The wide-area control signal can be further decomposed as

$$u_{\text{wac}}(t) = u_{\text{wac}}^{(\text{loc})}(t) + u_{\text{wac}}^{(\text{rem})}(t) \quad (11)$$

where $u_{\text{wac}}^{(\text{loc})}(t)$ corresponds to block-diagonal state feedback, and $u_{\text{wac}}^{(\text{rem})}(t)$ corresponds to feedback that utilizes the remote measurement signal $\theta_9(t)$ (which has to be communicated to the AVR controller at generator 1). Since the block-diagonal state feedback $u_{\text{wac}}^{(\text{loc})}(t)$ depends only on generator internal states, it can be implemented locally. The required generator state variables can be reconstructed online using appropriate filters and readily available measurements [48].

For the wide-area controller $u_{\text{wac}}(t) = -K_1^* x(t)$, if the local control $u_{\text{wac}}^{(\text{loc})}(t)$ is absorbed in the plant, then we obtain a 58.303° phase margin with respect to the remote control input $u_{\text{wac}}^{(\text{rem})}(t)$. The corresponding tolerable time-delay margin is 3.964 s. From a simulation of the linearized power grid model (2), we observe that a delay of 750 ms of the remote feedback signal $u_{\text{wac}}^{(\text{rem})}(t)$ does not significantly affect the closed-loop performance; see Fig. 8(c) and 8(f). In the delayed case, only a slight distortion of the trajectories of generator 1 [which is implementing the remote WAC signal $u_{\text{wac}}^{(\text{rem})}(t)$] is noticed.

Additionally, we found that the information structure identified by the WAC feedback $u_{\text{wac}}(t) = -K_1^* x$ is not sensitive to the actual operating and linearization point in the dynamics (1). To validate this hypothesis, we randomly altered the power demand at each load to create different loading conditions and operating points. Additionally, we perturbed the nominal PSS gains in (10). As a result, even if the PSS gains are randomly altered by factors within $[0.5, 4]$, and the load power demand is randomly altered within $\pm 25\%$ of the nominal demand [leading to different linearization matrices in (2)], the sparsity pattern of K_1^* is identical to the one shown in Fig. 5.

We conclude that the feedback resulting from the sparsity-promoting optimal control problem (6) is not only characterized by low communication requirements and good closed-loop performance but also by favorable robustness margins.

D. Sparsity Identification and Alternative Control Schemes

We note that while the local state feedback $u_{\text{wac}}^{(\text{loc})}(t)$ essentially requires a retuning of the local generator excitation control, the remote control signal $u_{\text{wac}}^{(\text{rem})}(t)$ needs to be communicated. Recall that one of our motivations for the sparsity-promoting optimal control formulation (6)—besides finding a sta-

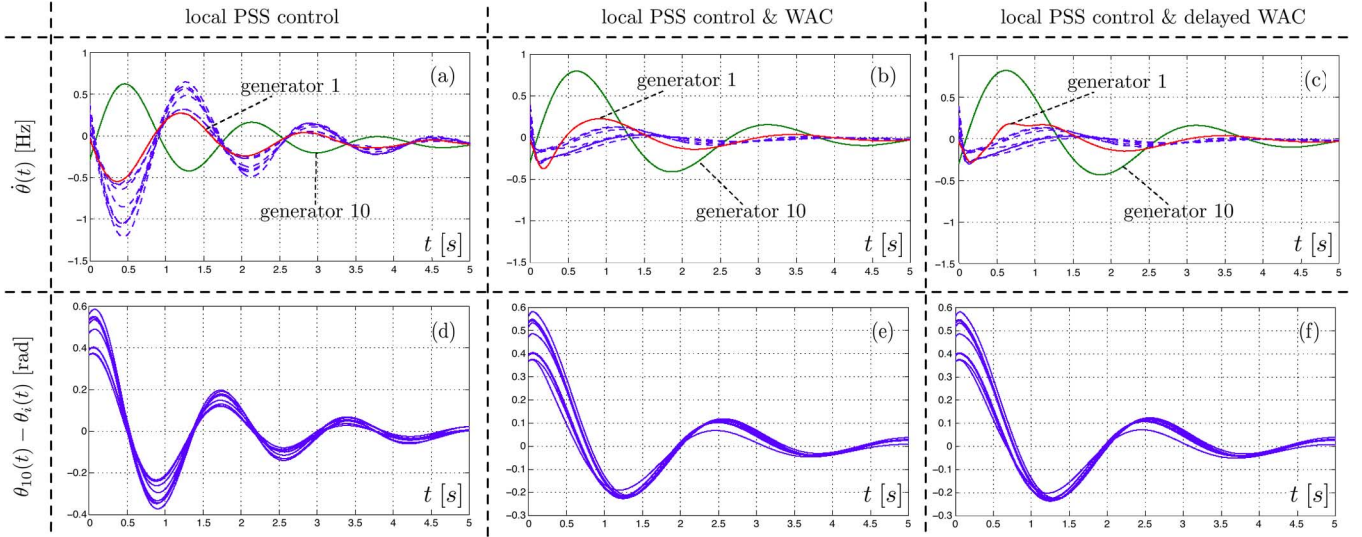


Fig. 8. Time-domain simulation of the linearized model (2) for the New England power grid: The subfigures show the generator frequencies and the angle differences (corresponding to inter-area power transfers) resulting from the use of only local PSS control, local PSS control and WAC (with the WAC signal $u_{wac}(t)$), and local PSS control and delayed WAC (with the remote WAC signal $u_{wac}^{(rem)}(t)$ from (11) being delayed by 750 ms). The initial conditions are aligned with the eigenvector of the dominant open-loop inter-area mode 1, and $u_{wac}(t)$ is subject to additive white noise with zero mean and standard deviation 0.01.

bilizing, robust, and optimal feedback—was the *identification* of an appropriate WAC architecture: which remote measurements need to be accessed by which controller?

For the considered model, our sparsity-promoting optimization framework identified a single crucial WAC channel: the rotor angle $\theta_9(t)$ serves as measurement to the AVR control at generator 1. After having identified this WAC channel, alternative control schemes can be developed. For instance, in absence of the local “retuning” control $u_{wac}^{(loc)}(t)$, the WAC feedback signal $u_{wac}(t)$ reduces to the proportional feedback

$$u_{wac}^{(rem)}(t) = [k(\theta_9(t) - \theta_1(t)) \ 0 \ \cdots \ 0]^T. \quad (12)$$

Here, $k > 0$ is the (1,9) element of K_1^* and we use the local rotor angle $\theta_1(t)$ as a reference for $\theta_9(t)$. Hence, no absolute angle measurements are required,⁵ and the WAC control (12) can be implemented, for example, by integrating the frequency difference $\dot{\theta}_9(t) - \dot{\theta}_1(t)$. The simple yet crucial proportional remote control signal (12) together with an appropriate retuning of the local PSSs (10) then yields the WAC signal $u_{wac}(t)$.

To illustrate the utility of our sparsity-promoting identification scheme, we apply the proportional WAC signal (12) to the full nonlinear differential-algebraic power network model (1) equipped with the PSSs (10). To demonstrate the importance of the WAC channel $9 \rightarrow 1$, we do not re-tune the local PSSs to emulate $u_{wac}^{(loc)}(t)$. We verify that the WAC signal (12) does not lead to a loss of small-signal stability, and we investigate the performance of the closed-loop using time-domain simulations in Fig. 10. Our simulation scenario is based on a three phase fault at line {3,4} at 0.1 s, which is cleared at 0.2 s. The WAC input (12) is subject to a delay of 750 ms. In analogy to the linear simulation in Fig. 8, we compare the system responses with and without the WAC signal (12) both with and without

⁵Indeed, in the limit $\varepsilon \searrow 0$ in the cost functions (8), (9), the solution to the optimal control problem (7) features a rotational symmetry, and the control input requires only angular differences rather than absolute angles.

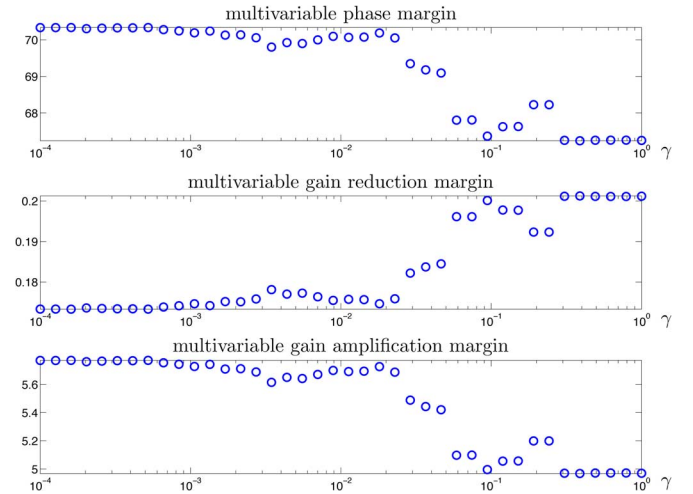


Fig. 9. Multivariable phase and gain margins achieved by the optimal sparsity-promoting controller as a function of γ .

a 750 ms delay. As in the linearized case, the decay rates of the frequencies are comparable but the inter-area modes are distorted in WAC closed loop; see Fig. 10(a) and 10(b). Due to the lack of tuned local feedback $u_{wac}^{(loc)}(t)$ in (12), generator 10 still slightly swings against the remaining generators in WAC closed loop. On the other hand, the implementation of the WAC signal (12) by generator 1 results in a reduced effort in providing stabilizing control signals; see Fig. 10(d) and 10(e). These conclusions also hold in presence of a severe delay, as seen in Fig. 10(c) and 10(f). As compared to the linear case [including the local feedback $u_{wac}^{(loc)}(t)$] shown in Fig. 8, the nonlinear performance [without local feedback $u_{wac}^{(loc)}(t)$] is not insensitive to delays and slightly degrades. To further account for communication delays, a local control $u_{wac}^{(loc)}(t)$ can be added, and the remote proportional WAC feedback signal (12) can be fed through a delay-compensating filter as in [21].

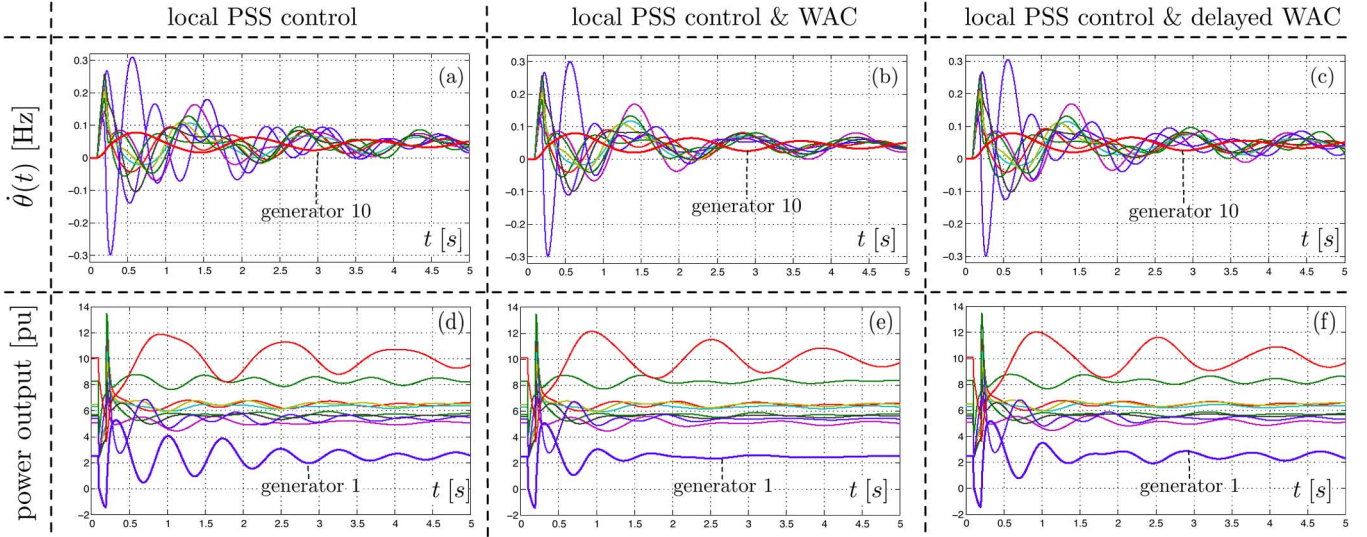


Fig. 10. Time-domain simulation of the full nonlinear differential-algebraic model (1) for the New England power grid: The subfigures show the generator frequencies and active power outputs using only local PSS control and using the remote WAC signal $u_{\text{wac}}^{(\text{rem})}(t)$ both without delay and with a 750 ms delay. Initially, the system is at steady state, and a three phase fault at line $\{3, 4\}$ at 0.1 s, which is cleared at 0.2 s.

We conclude that the simple proportional feedback (12) identified by the sparsity-promoting framework significantly improves the closed-loop performance. We note that the proportional WAC strategy (12) merely serves as an illustration of the ability of our method to identify a suitable WAC architecture. Now that the crucial WAC channel $9 \rightarrow 1$ has been identified, more sophisticated single-input-single-output control strategies can be developed via alternative means.

IV. CONCLUSIONS

We proposed a novel approach to wide-area control of inter-area oscillations. We followed a recently introduced paradigm to sparsity-promoting optimal control [37]. Our performance objectives were inspired by the well-known slow coherency theory. We validated the proposed control strategy on the IEEE 39 New England power grid model, which demonstrated nearly optimal performance, low communication requirements, and robustness of the sparsity-promoting controller.

Of course, further scrutiny of the proposed sparsity-promoting framework on other power system models is needed. We note that both the structure and the performance achieved by our sparsity-promoting controller are problem-dependent: they are influenced by the model of the underlying power system as well as by the selection of state and control weights. For the considered IEEE 39 New England model, we have illustrated the insensitivity of the identified controller structure on the operating point and the graceful performance degradation relative to the optimal centralized controller. In our future effort, we will examine if these properties also hold for other power systems and investigate how the resulting controller structure is influenced by the system's dynamics.

Our initial results are very promising, and we are currently working on further extensions. The authors also envision an application of the proposed control strategy to enhance the performance of purely decentralized primary and secondary control schemes [49] with supplementary WAC. Since sparsity is

a function of the state space coordinates, the identified control scheme may not be sparse in other coordinates. Hence, an interesting question is to identify state space representations of power system models, which are amenable to a sparsity-promoting control design. For example, it is of interest to extend the proposed design methodology to sparse, differential-algebraic, and structure-preserving models. Finally, the authors also aim to gain insight into fundamental performance limitations induced by localized and wide-area control strategies.

APPENDIX

A. Algorithmic Methods for Sparsity-Promoting Optimization

We briefly summarize the algorithmic approach to the optimization problem (7) and refer to [37] for further details:

- 1) **Warm-start and homotopy:** The optimal control problem (7) is solved by tracing a homotopy path that starts at the optimal centralized controller with $\gamma = 0$ and continuously increases γ until the desired value γ_{des} .
- 2) **ADMM:** For each value of $\gamma \in [0, \gamma_{\text{des}}]$, the optimization problem (7) is solved iteratively using ADMM;
- 3) **Updates of weights:** In each step of ADMM, the weights are updated as $w_{ij} = 1/(|K_{ij}| + \varepsilon)$ with $\varepsilon > 0$. We have conducted 5 update steps with $\varepsilon = 10^{-3}$; and
- 4) **Polishing:** Once the desired sparsity pattern \mathcal{K} is identified, a structured optimal control problem is solved:

$$\begin{aligned} & \text{minimize} \quad J_\gamma(K) = \text{trace}(B_1^T P B_1) \\ & \text{subject to} \quad K \in \mathcal{K}, \\ & \quad (A - B_2 K)^T P + P(A - B_2 K) = -(Q + K^T R K). \end{aligned}$$

This iterative approach is convergent under a local convexity assumption, and stability of $A - B_2 K$ is guaranteed. The algorithms developed in [37] have been implemented in *MATLAB*. The associated software as well as the numerical power network data used in the present paper can be downloaded at <http://www.ece.umn.edu/users/mihailo/software/lqrsp/>.

ACKNOWLEDGMENT

The authors would like to thank S. Dhople for helpful comments on an early version of this paper and S. Ghiocel for helpful discussions regarding the Power Systems Toolbox.

REFERENCES

- [1] F. Dörfler, M. Jovanović, M. Chertkov, and F. Bullo, "Sparse and optimal wide-area damping control in power networks," in *Proc. Amer. Control Conf.*, Washington, DC, USA, Jun. 2013, pp. 4295–4300.
- [2] V. Venkatasubramanian and Y. Li, "Analysis of 1996 Western American electric blackouts," in *Proc. Bulk Power System Dynamics and Control-VI*, Cortina d'Ampezzo, Italy, 2004.
- [3] P. Kundur, *Power System Stability and Control*. New York, NY, USA: McGraw-Hill, 1994.
- [4] R. Grondin, I. Kamwa, L. Soulières, J. Potvin, and R. Champagne, "An approach to PSS design for transient stability improvement through supplementary damping of the common low-frequency," *IEEE Trans. Power Syst.*, vol. 8, no. 3, pp. 954–963, Aug. 1993.
- [5] I. Kamwa, J. Beland, G. Trudel, R. Grondin, C. Lafond, and D. McNabb, "Wide-area monitoring and control at Hydro-Québec: Past, present and future," in *Proc. IEEE Power & Energy Society General Meeting*, 2006, p. 12.
- [6] J. H. Chow, J. J. Sanchez-Gasca, H. Ren, and S. Wang, "Power system damping controller design—using multiple input signals," *IEEE Control Syst. Mag.*, vol. 20, no. 4, pp. 82–90, 2000.
- [7] N. Martins and L. T. G. Lima, "Eigenvalue and frequency domain analysis of small-signal electromechanical stability problems," in *Proc. IEEE/PES Symp. Applications of Eigenanalysis and Frequency Domain Methods*, 1989, pp. 17–33.
- [8] R. A. Jabr, B. C. Pal, N. Martins, and J. C. R. Ferraz, "Robust and coordinated tuning of power system stabiliser gains using sequential linear programming," *IET Gen., Transm., Distrib.*, vol. 4, no. 8, pp. 893–904, 2010.
- [9] K. Seethalekshmi, S. N. Singh, and S. C. Srivastava, "Wide-area protection and control: Present status and key challenges," in *Proc. 15th National Power Systems Conf.*, Bombay, India, Dec. 2008, pp. 169–175.
- [10] J. Xiao, F. Wen, C. Y. Chung, and K. P. Wong, "Wide-area protection and its applications—a bibliographical survey," in *Proc. IEEE PES Power Systems Conf. Expo.*, Atlanta, GA, USA, Oct. 2006, pp. 1388–1397.
- [11] Y. Chompoobutgool, L. Vanfretti, and M. Ghandhari, "Survey on power system stabilizers control and their prospective applications for power system damping using synchrophasor-based wide-area systems," *Eur. Trans. Elect. Power*, vol. 21, no. 8, pp. 2098–2111, 2011.
- [12] M. Amin, "Special issue on energy infrastructure defense systems," *Proc. IEEE*, vol. 93, no. 5, pp. 855–860, 2005.
- [13] Q. Liu, V. Vittal, and N. Elia, "LPV supplementary damping controller design for a thyristor controlled series capacitor (TCSC) device," *IEEE Trans. Power Syst.*, vol. 21, no. 3, pp. 1242–1249, Aug. 2006.
- [14] K. Tomovic, D. E. Bakken, V. Venkatasubramanian, and A. Bose, "Designing the next generation of real-time control, communication, and computations for large power systems," *Proc. IEEE*, vol. 93, no. 5, pp. 965–979, 2005.
- [15] A. Chakraborty, "Wide-area damping control of power systems using dynamic clustering and TCSC-based redesigns," *IEEE Trans. Smart Grid*, vol. 3, no. 3, pp. 1503–1514, 2012.
- [16] M. Zima, M. Larsson, P. Korba, C. Rehtanz, and G. Andersson, "Design aspects for wide-area monitoring and control systems," *Proc. IEEE*, vol. 93, no. 5, pp. 980–996, 2005.
- [17] G. E. Boukarim, S. Wang, J. H. Chow, G. N. Taranto, and N. Martins, "A comparison of classical, robust, and decentralized control designs for multiple power system stabilizers," *IEEE Trans. Power Syst.*, vol. 15, no. 4, pp. 1287–1292, Nov. 2000.
- [18] Y. Zhang and A. Bose, "Design of wide-area damping controllers for interarea oscillations," *IEEE Trans. Power Syst.*, vol. 23, no. 3, pp. 1136–1143, Aug. 2008.
- [19] B. Chaudhuri, R. Majumder, and B. C. Pal, "Wide-area measurement-based stabilizing control of power system considering signal transmission delay," *IEEE Trans. Power Syst.*, vol. 19, no. 4, pp. 1971–1979, Nov. 2004.
- [20] A. Chakraborty, J. H. Chow, and A. Salazar, "A measurement-based framework for dynamic equivalencing of large power systems using wide-area phasor measurements," *IEEE Trans. Smart Grid*, vol. 2, no. 1, pp. 56–69, 2011.
- [21] P. Zhang, D. Yang, K. Chan, and G. Cai, "Adaptive wide-area damping control scheme with stochastic subspace identification and signal time delay compensation," *IET Gen., Transm., Distrib.*, vol. 6, no. 9, pp. 844–852, 2012.
- [22] R. Eriksson and L. Soder, "Wide-area measurement system-based subspace identification for obtaining linear models to centrally coordinate controllable devices," *IEEE Trans. Power Del.*, vol. 26, no. 2, pp. 988–997, Apr. 2011.
- [23] Y. Pipelzadeh, B. Chaudhuri, and T. Green, "Wide-area power oscillation damping control through hvdc: A case study on Australian equivalent system," in *Proc. 2010 IEEE Power and Energy Society General Meeting*, 2010, pp. 1–7.
- [24] S. Skogestad and I. Postlethwaite, *Multivariable Feedback Control Analysis and Design*, 2nd ed. New York, NY, USA: Wiley, 2005.
- [25] A. Heniche and I. Kamwa, "Control loops selection to damp inter-area oscillations of electrical networks," *IEEE Trans. Power Syst.*, vol. 17, no. 2, pp. 378–384, May 2002.
- [26] H. Nguyen-Duc, L. Dessaint, A. F. Okou, and I. Kamwa, "Selection of input/output signals for wide area control loops," in *Proc. IEEE Power & Energy Society General Meeting*, Minneapolis, MN, USA, Jul. 2010, pp. 1–7.
- [27] L. P. Kunjumammed, R. Singh, and B. C. Pal, "Robust signal selection for damping of inter-area oscillations," *IET Gen., Transm., Distrib.*, vol. 6, no. 5, pp. 404–416, 2012.
- [28] B. Eliasson and D. Hill, "Damping structure and sensitivity in the Nordel power system," *IEEE Trans. Power Syst.*, vol. 7, no. 1, pp. 97–105, Feb. 1992.
- [29] A. Heniche and I. Kamwa, "Assessment of two methods to select wide-area signals for power system damping control," *IEEE Trans. Power Syst.*, vol. 23, no. 2, pp. 572–581, May 2008.
- [30] F. Lin, M. Fardad, and M. R. Jovanović, "Augmented Lagrangian approach to design of structured optimal state feedback gains," *IEEE Trans. Automat. Control*, vol. 56, no. 12, pp. 2923–2929, 2011.
- [31] A. Mahajan, N. C. Martins, M. C. Rotkowitz, and S. Yuksel, "Information structures in optimal decentralized control," in *Proc. IEEE Conf. Decision and Control*, Maui, HI, USA, Dec. 2012, pp. 1291–1306.
- [32] S. Schuler, U. Münz, and F. Allgöwer, "Decentralized state feedback control for interconnected systems with application to power systems," *J. Process Control*, to be published.
- [33] S. Schuler, U. Münz, and F. Allgöwer, "Decentralized state feedback control for interconnected process systems," in *Proc. IFAC Symp. Advanced Control of Chemical Processes*, Furama Riverfront, Singapore, Jul. 2012, pp. 1–10.
- [34] U. Münz, M. Pfister, and P. Wolfrum, "Sensor and actuator placement for linear systems based on H_2 and H_∞ optimization," *IEEE Trans. Automat. Control*, to be published.
- [35] M. Fardad, F. Lin, and M. R. Jovanović, "Sparsity-promoting optimal control for a class of distributed systems," in *Proc. Amer. Control Conf.*, San Francisco, CA, USA, Jun. 2011, pp. 2050–2055.
- [36] F. Lin, M. Fardad, and M. R. Jovanović, "Sparse feedback synthesis via the alternating direction method of multipliers," in *Proc. Amer. Control Conf.*, Montréal, QC, Canada, Jun. 2012, pp. 4765–4770.
- [37] F. Lin, M. Fardad, and M. R. Jovanović, "Design of optimal sparse feedback gains via the alternating direction method of multipliers," *IEEE Trans. Automat. Control*, vol. 58, no. 9, pp. 2426–2431, Sep. 2013.
- [38] D. L. Donoho, "Compressed sensing," *IEEE Trans. Inf. Theory*, vol. 52, no. 4, pp. 1289–1306, 2006.
- [39] J. H. Chow, *Time-Scale Modeling of Dynamic Networks With Applications to Power Systems*. New York, NY, USA: Springer, 1982.
- [40] J. H. Chow and P. Kokotović, "Time scale modeling of sparse dynamic networks," *IEEE Trans. Automat. Control*, vol. 30, no. 8, pp. 714–722, 1985.
- [41] D. Romeres, F. Dörfler, and F. Bullo, "Novel results on slow coherency in consensus and power networks," in *Proc. European Control Conf.*, Zürich, Switzerland, Jul. 2013.
- [42] F. Dörfler and F. Bullo, "Kron reduction of graphs with applications to electrical networks," *IEEE Trans. Circuits Syst. I: Reg. Papers*, vol. 60, no. 1, pp. 150–163, 2013.
- [43] E. J. Candès, M. B. Wakin, and S. P. Boyd, "Enhancing sparsity by reweighted ℓ_1 minimization," *J. Fourier Anal. Applicat.*, vol. 14, no. 5, pp. 877–905, 2008.

- [44] B. Bamieh and D. F. Gayme, "The price of synchrony: Resistive losses due to phase synchronization in power networks," in *Proc. Amer. Control Conf.*, Washington, DC, USA, Jun. 2013.
- [45] M. Safonov and M. Athans, "Gain and phase margin for multiloop LQG regulators," *IEEE Trans. Automat. Control*, vol. 22, no. 2, pp. 173–179, 1977.
- [46] J. Doyle and G. Stein, "Multivariable feedback design: Concepts for a classical/modern synthesis," *IEEE Trans. Automat. Control*, vol. 26, no. 1, pp. 4–16, 1981.
- [47] J. H. Chow and K. W. Cheung, "A toolbox for power system dynamics and control engineering education and research," *IEEE Trans. Power Syst.*, vol. 7, no. 4, pp. 1559–1564, Nov. 1992.
- [48] K. Zhang, X. Dai, and C. Huang, "Left-inversion soft-sensor of synchronous generator," *Int. Trans. Elect. Energy Syst.*, vol. 23, no. 1, pp. 48–61, 2013.
- [49] K. Dvijotham, S. Backhaus, and M. Chertkov, "Distributed control of generation in a transmission grid with a high penetration of renewables," in *Proc. IEEE Int. Conf. Smart Grid Communications*, Tainan City, Taiwan, Nov. 2012, pp. 635–640.



Florian Dörfler (S'09–M'13) received the Diplom degree in engineering cybernetics from the University of Stuttgart, Germany, in 2008 and the Ph.D. degree in mechanical engineering from the University of California at Santa Barbara in 2013.

He is an Assistant Professor in the Department of Electrical Engineering at the University of California Los Angeles, and he is affiliated with the Center for Nonlinear Studies at the Los Alamos National Laboratories. His primary research interests are centered around distributed control, complex networks, and

cyber-physical systems with applications to smart power grids and robotic coordination.

Prof. Dörfler is recipient of the 2009 Regents Special International Fellowship, the 2011 Peter J. Frenkel Foundation Fellowship, the 2010 ACC Student Best Paper Award, and the 2011 O. Hugo Schuck Best Paper Award. As a co-advisor and a co-author, he has been a finalist for the ECC 2013 Best Student Paper Award.



Mihailo R. Jovanović (S'00–M'05–SM'13) received the Dipl. Ing. and M.S. degrees from the University of Belgrade, Serbia, in 1995 and 1998, respectively, and the Ph.D. degree from the University of California, Santa Barbara, in 2004, under the direction of Bassam Bamieh.

Before joining the University of Minnesota, Minneapolis, he was a Visiting Researcher with the Department of Mechanics, the Royal Institute of Technology, Stockholm, Sweden, from September to December 2004. Currently, he is an Associate Professor of electrical and computer engineering at the University of Minnesota, Minneapolis, where he also serves as the Director of Graduate Studies in the interdisciplinary Ph.D. program in control science and dynamical systems. He has

held visiting positions with Stanford University and the Institute for Mathematics and its Applications. His expertise is in modeling, dynamics, and control of large-scale and distributed systems and his current research focuses on sparsity-promoting optimal control, dynamics and control of fluid flows, and fundamental performance limitations in the design of large dynamic networks.

Prof. Jovanovic is a member of APS and SIAM. He currently serves as an Associate Editor of the SIAM Journal on Control and Optimization and has served as an Associate Editor of the IEEE Control Systems Society Conference Editorial Board from July 2006 until December 2010. He received a CAREER Award from the National Science Foundation in 2007, an Early Career Award from the University of Minnesota Initiative for Renewable Energy and the Environment in 2010, a Resident Fellowship within the Institute on the Environment at the University of Minnesota in 2012, and the George S. Axelby Outstanding Paper Award from the IEEE Control Systems Society in 2013.



Michael Chertkov (M'04) received the M.Sc. degree in physics from Novosibirsk State University, Russia, in 1990 and the Ph.D. degree in physics from the Weizmann Institute of Science, Israel, in 1996.

After his Ph.D., he spent three years at Princeton University, Princeton, NJ, USA, as a R.H. Dicke Fellow in the Department of Physics. He joined Los Alamos National Lab in 1999, initially as a J. R. Oppenheimer Fellow in the Theoretical Division. He is now a technical staff member in the same division.

He has published more than 120 papers in these research areas. His areas of interest include statistical and mathematical physics applied to energy and communication networks, machine learning, control theory, information theory, computer science, fluid mechanics and optics.

Dr. Chertkov is an editor of the Journal of Statistical Mechanics (JSTAT), associate editor of IEEE TRANSACTIONS ON CONTROL OF NETWORK SYSTEMS, a fellow of the American Physical Society (APS), and a Founding Faculty Fellow of Skolkovotech—young graduate school built in Moscow, Russia.



Francesco Bullo (S'95–M'99–SM'03–F'10) is a Professor with the Mechanical Engineering Department and the Center for Control, Dynamical Systems and Computation at the University of California, Santa Barbara. He was previously associated with the University of Padova, the California Institute of Technology, and the University of Illinois at Urbana-Champaign. His main research interests are network systems and distributed control with application to robotic coordination, power grids and social networks. He is the coauthor of *Geometric Control of Mechanical Systems* (New York, NY, USA: Springer) and *Distributed Control of Robotic Networks* (Princeton, NJ, USA: Princeton Univ. Press, 2009).

Prof. Bullo has served on the editorial boards of: IEEE TRANSACTIONS ON AUTOMATIC CONTROL, ESAIM: Control, Optimization, and the Calculus of Variations, SIAM Journal of Control and Optimization, and Mathematics of Control, Signals, and Systems.