

Homework 6

Due: Tuesday, March 30, 11:15 AM

1. 12.3: Note that the corrected equation (12.17) is

$$\text{DFT}\{x[n] \otimes h[n]\} = \sqrt{N} \cdot \text{DFT}\{x[n]\} \cdot \text{DFT}\{h[n]\} \quad (1)$$

(The \sqrt{N} factor is missing in the book)

2. 12.7
3. 12.9: Replace \mathbf{H} with $\tilde{\mathbf{H}}$ throughout the problem.
4. 12.11: Replace \mathbf{H} with $\tilde{\mathbf{H}}$ in part (b).
5. 12.10
6. You are designing a 10 MHz OFDM system at a carrier frequency of 1 GHz. Assume that you are in an outdoor environment with a maximum delay spread of 15 microseconds.
 - (a) What length cyclic prefix is needed for this system?
 - (b) What is the efficiency of a system using 1024 subcarriers ($N = 1024$)?
 - (c) Repeat parts (a) and (b) for an indoor environment with a maximum delay spread of 1 microsecond.
7. In this problem we study the PAPR of the transmit samples (i.e., the outputs of the IFFT at the TX). In the notation from lecture, we used $\tilde{d}[0], \dots, \tilde{d}[N - 1]$ to denote the QAM symbols, while $d[0], \dots, d[N - 1]$ are the IFFT of the QAM symbols (i.e., the transmit samples). In terms of these discrete-time samples, the PAPR is:

$$\text{PAPR} = \frac{\max_{k=0, \dots, N-1} |d[k]|^2}{(1/N) \sum_{k=0}^{N-1} |d[k]|^2} \quad (2)$$

This quantity depends on the values $d[0], \dots, d[N - 1]$, which are in turn determined by the N data symbols $\tilde{d}[0], \dots, \tilde{d}[N - 1]$. Thus, we can think of PAPR as a random variable, where the randomness originates from the randomness in the data symbols.

In this problem you are to write a Matlab program that numerically generates the CCDF (one minus the CDF) of random variable PAPR. Assume that the N data symbols are chosen in an iid fashion from a 4-QAM constellation.

- (a) Create a plot of the PAPR (in dB) versus the CCDF (i.e., the probability that PAPR is larger than the value on the x-axis) for $N = 16$, $N = 64$, and $N = 1024$.

(b) Comment on how likely it is that the PAPR is the worst-case of N .

Note: In theory you could determine the exact distribution of PAPR by going through all 4^N different data symbol combinations. However, this is computationally impossible except when N is very small. Thus, you should generate the CDF by trying a very large number of random data symbol combinations (i.e., use Monte Carlo simulation).