# Automated synthesis of mixed-signal ML inference hardware under accuracy constraints

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Abstract—Due to the inherent error-tolerance of machine learning (ML) algorithms, many parts of the inference computation can be performed with adequate accuracy and low power under relatively low precision. Early approaches have used digital approximate computing methods to explore this space. Recent approaches using analog-based operations achieve power-efficient computation at moderate precision. This work proposes a mixed-signal optimization (MiSO) approach that optimally blends analog and digital computation for ML inference. Based on accuracy and power models, an integer linear programming formulation is used to optimize design metrics of analog/digital implementations. The efficacy of the method is demonstrated on multiple ML architectures.

## I. INTRODUCTION

Machine learning (ML) hardware requires high energy-efficiency, but is primarily built using digital circuits today. For low-to-moderate precision tasks, at iso-precision, analog circuits are much more energy-efficient than their digital counterparts [1], [2]. The selective use of analog computing is thus an excellent fit for ML, where lower precision can be used for less sensitive operations without harming overall accuracy; for sensitive operations that require high precision, digital circuitry may be used. There has been no systematic EDA exploration of this tradeoff space to achieve optimal energy-efficiency.

DNN models are resilient to small computation errors, and this has been widely exploited to optimize digital ML hardware through lowprecision fixed-point computations [3], approximate computing [4], and model compression [5]. There has been also work on specialized hardware for energy optimization of these quantized models [6]. Analog approaches often target small networks/datasets [7], [8]; those that address larger networks [9], [10] focus on **single-layered** analog operations, adding an analog-to-digital/digital-to-analog converter (ADC/DAC) after each simple analog operation. This results in massive ADC/DAC energy overheads. To amortize these costs, approaches such as interleaved bit-partitioning, or a combination of digital and charge-domain accumulation are proposed [9], [10], but data conversion costs remain a major system-level consideration.

We propose MiSO-ML (Mixed Signal Optimization for low-power ML), which builds optimal hardware architectures that bring the best of both worlds, analog and digital, for energy-efficient ML inference. We create energy and noise models for fundamental analog and digital operations, at different precision levels. Using these models, our system-level optimization creates energy-efficient hardware under an accuracy specification. Unlike prior single-layered approaches, we amortize the cost of ADCs/DACs across multiple layers of an ML architecture. This provides significant energy efficiency benefits, reducing data conversion overhead to just 13.2% (as opposed to 52.2% in [11]) while harnessing the efficiency gains of mixed-signal computation. The contributions of MiSO-ML are listed below:

- We propose a framework for optimizing ML models for low power using mixed-signal computing.
- 2) We propose a novel hardware-aware mixed-precision quantization using an integer linear programming (ILP) formulation

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to find an optimal bit-precision setting, and to optimize the ADC overhead by performing analog-to-digital conversions after multiple layers, when possible within noise constraints.

 We demonstrate substantial power improvement on common ML-architectures, as compared to a digital-only quantization.

Intuitive concept. When ML operations are performed using analog circuits, they inevitably accumulate an analog noise voltage,  $V_n$ , that acts as an offset to the equivalent digital value. Since the resolution of an ADC is 0.5 LSB (least-significant bit), as long as the analog computation is recoverted to digital form while  $V_n < 0.5$  LSB, the signal is "restored" to full digital precision, with no accuracy loss [1]. Firstly, our optimization scheme tracks the maximum noise over multiple layers of a DNN, and finds that one can often introduce ADCs after multiple layers of DNN computation. This allows the cost of data conversion to be amortized over multiple layers, unlike [7], [8]. Secondly, we optimize the precision for each layer: typically, 8-bit precision requires an ADC after each layer, but relaxed precision allows greater amortization, and with the right optimization, does not significantly affect accuracy. Our approach is guided by a metric of sensitivity of the output to noise in an operation, driving noise-sensitive computations to be performed in digital or higher precision analog modes, an less sensitive operations using analog circuits at lower precision. Through these ILP-based optimizations, we demonstrate large gains from mixed-signal computing.

Next, in Section II, we propose our building block module, a foundational element for modeling a range of digital/analog operations. Section III delves into the modeling of energy and noise values for various state-of-the-art computation operations; Section IV then models the propagation of noise propagation from digital/analog operations across layers in an ML architecture. These are used to build energy lookup table and noise sensitivity models for ML architectures in Section V, and invoked in our ILP-based approach in Section VI. Finally, Section VII evaluates MiSO-ML across several ML architectures, and Section VIII concludes this article.

#### II. PROPOSED MIXED-SIGNAL ML HARDWARE SCHEME

To extend analog computations to deeper architectures with a diverse set of operations, hybrid computation is necessary, in which analog processing must be followed by restoration of the analog signal to discrete values to overcome noise accumulation problems. As pointed out above, the high energy overhead of these domain-switching operations (using ADCs/DACs) must be balanced with the amount of noise accumulation over multiple analog stages.

For this optimization, we propose a building block (Fig. 1) to map operations from ML architectures, leveraging multiple stacked analog operations before the conversion to the digital domain. This block takes two input operands (e.g., weight and activation), and generates its output after performing the operation. For each operation, we have three optimization parameters: (1) the operation domain (digital or analog), (2) the operation precision, and (3) the presence/absence of a data converter (ADC or DAC), required when the input signal



Figure 1: Building block diagram of the MiSO-ML unit.



Figure 2: Hardware mapping of a CNN architecture by MiSO-ML.

domain differs from the operation domain. Based on a data-flow graph (DFG), created by mapping all operations from the input architecture to the building block model, we optimize the energy of the hardware implementation using an ILP solver. In a post-processing step for multiple fan-out nodes, multiple data converters are merged.

For example, in an analog sum operation, digital weights and activations from memory are first converted into the analog domain using DACs. Next, the addition is performed using charge sharing [12]. The analog output is sent out to the next stage, where it may be passed through an analog max-pooling operation and an analog sigmoid/tanh operator without any data domain conversion. Multiple such analog stages can be cascaded, with the total noise increasing as more stages are cascaded, until the noise reaches the threshold level of requisite precision. The MiSO-ML unit block includes data conversion (ADC/DAC), which enables the ability to handle individual operations as well as complex operations with specialized circuits, e.g., digital-to-analog MAC operations [9], [13].

Fig. 2 shows a CNN architecture being mapped to hardware by MiSO-ML. The convolution operation is mapped to analog MAC hardware with 4-bit precision, whose results are fed through an analog max-pooling circuit with 4-bit precision before being converted to the digital domain. Next, the fully-connected layer is mapped to digital MAC hardware with 6-bit precision and is then sent to ReLU hardware with 6-bit precision. In this hardware mapping, the input features size is larger thus larger number of operations (21600 MAC + 216 Max-pool) are performed in the analog domain and very few (432 MAC + 2 ReLU) operations are carried out in the digital domain, thus improving the energy cost of this model over a purely digital implementation, even after including the cost of the ADC operations.

# **III. ANALYTICAL ENERGY AND ERROR MODELS**

# A. Digital computations: quantization models

Energy models for digital computation blocks are well understood [4], [6], [14], [15], and are summarized in Section V. We focus here on the impact of bitwidth-dependent quantization in digital blocks on error. The error arising from quantizing analog signals in an ADC, relative to the signal strength, is quantified as signal-to-quantization noise ratio (SQNR), where quantization noise reflects the loss in accuracy due to quantization. For *B* bits of precision, the SQNR is [16]:

$$SQNR = 1.76 + 6.02B$$
 (1)



**Figure 3:** Implementation of addition operation (a) circuit diagram of addition operation using charge sharing [12], and (b) circuit diagram of passive analog MAC implementations [17].

Thus, to achieve an extra bit of precision, the signal-to-noise ratio (SNR $\approx$ SQNR) of the system should increase by 6.02 dB, i.e., it should approximately double. Thus, for the same signal, reducing digital precision by one bit increases noise by  $\approx 2 \times$ .

#### B. Analog computations: Noise and energy models

Mapping an ML algorithm to hardware requires hardware blocks for multiple types of operations such as MAC, sum, linear scaling, ReLU/sigmoid/tanh, and max-pooling. We analyze analog building blocks for these operations and present their energy and noise models. <u>Sources of variation</u>. There are several sources of noise in analog circuits. **Process-induced drifts and parasitic effects can largely be canceled out** [17] by using state-of-the-art precise sub-femtofarad capacitors with 1% standard deviation (in active switched-capacitorbased structures) and differential structures. This leaves intrinsic mechanisms, i.e., thermal noise and 1/f flicker noise: at >100 MHz, as in this work, *thermal noise is the dominant contributor* [16].

In resistors, the thermal noise voltage is proportional to  $\sqrt{kTR}$ , where k is Boltzmann's constant, T is the temperature, and R is the resistance. In switched capacitor circuits (which we will use extensively), the RMS thermal noise is proportional to  $\sqrt{kT/C}$ (and independent of R [16]). To improve the precision of switched capacitor networks by one bit,  $\sqrt{kT/C}$  must be halved: thus, every bit of precision requires  $4 \times larger$  capacitors, with  $4 \times$  higher energy. This makes analog circuits unsuitable for high precision, but for < 8bit precision, analog implementations remain attractive [1].

1) Addition/subtraction: Addition can be performed in the analog domain using charge sharing [12], as illustrated in Fig. 3(a). Initially, the switch is open and the operands are loaded as analog voltages on the capacitors. When the switch is closed, the operands are averaged, thus implementing a scaled addition operation. The energy consumed in the circuit is the switching energy for the transistor, used to charge/discharge the gate capacitors. The energy and noise are given by:

$$E_{ADD} = E_{switch} + C(V_a^2 + V_b^2);$$
  $N_{ADD} = 2kT/C$ 

2) Analog multiplication: Matrix multiplication  $(y = Ax, x \in \mathbb{R}^n, y \in \mathbb{R}^m, A \in \mathbb{R}^{m \times n})$ , is a fundamental operation in ML that has been traditionally realized by MAC units. We explore two analog multipliers [17], with analog or digital inputs, and an analog output. Analog input voltage MAC (AMAC): In ML hardware, the weights are typically stored in digital form. For a MAC operation with analog inputs, we use a highly energy-efficient switched-capacitor matrix multiplier as shown in Fig. 3(b) [17]. Here  $C_1$  is a capacitive DAC that is controlled based on the weights stored in the memory. In the first phase  $(\Phi_1)$ , the input voltage  $V_x$  is multiplied by  $C_1$ , and in the second phase  $(\Phi_2)$ , the multiplied charge  $V_xC_1$  is redistributed on capacitor  $C_2$ . For an N-dimensional inner product, this operation is performed N times such that  $V_{C_2} = (1/C_2) \sum_{i=1}^{N} V_x[i]C_1[i]$ . For low-resolution multiplication,  $C_2 \gg C_1$ , i.e., for 3-bit precision,  $C_2$ is  $39 \times$  larger than the maximum  $C_1$ , and for every bit of precision, we increase the size of  $C_2$  by  $4 \times$  to overcome thermal noise. The total energy is the sum of the energy dissipated in the capacitors and in the switches. The energy and noise equations for this circuit are:

$$E_{AMAC} = 4E_{switch} + (C_1 + C_2)V_{DD}^2; \quad N_{AMAC} \approx kT/C_2$$
 (2)

where  $E_{switch}$  is the average energy dissipated in charging/discharging the gate capacitor of each of the four switches and  $C_2 \gg C_1$ .

Digital input voltage MAC (DMAC): When both the weights and the signal are digital, one option is to convert the data input to an analog value using a DAC, and then use the analog MAC as explained in the previous paragraph. In some cases, the digital properties of the signal can be utilized to perform a bit-wise product to reduce the energy loss in the DAC capacitance. In [9], XNOR gates are used for bitwise multiplication, reducing the energy consumed in the DACs. The noise in this operation comes from digital quantization noise and from thermal noise (kT/C) from the switching of the unit capacitors connected to the output of XNOR gates. The energy consumption and noise for this circuit for a *B*-bit operation is given by:

$$E_{DMAC} = B^2 \alpha (E_{switch} + C_u V_{DD}^2); \ N_{DMAC} = kT/(2^B C_u) \ (3)$$

3) Max-pooling operation: Pooling layers downsample features to reduce the computational burden on subsequent layers. Two common pooling methods are average- and max-pooling. Average-pooling can be implemented using the sum operation described earlier, and maxpooling can be implemented using a voltage-mode-max circuit [18].

Using transistor noise equations for a single pooling operation, energy and noise are a function of the signal path current  $(I_D)$ :

$$E_{pool} = 2I_D V_{DD}; \quad N_{pool} \approx K' / I_D \tag{4}$$

where K' is derived using the circuit topology and device sizes. 4) Activation functions: ML models use nonlinear activation functions such as ReLU, tanh, and sigmoid. The ReLU function selects the maximum of the input signal and the reference (usually 0), and thus max-pooling circuits can implement ReLU. A tanh or sigmoid function can be realized by a common-source differential amplifier by leveraging intrinsic transistor nonlinearity [19].<sup>1</sup> The total energy and output-referred noise of the 5T-OTA circuit is [19]:

$$E_{\text{sigmoid}} = 2I_D V_{DD}; N_{\text{sigmoid}} = 32kT n_f (V_{gs} - V_{th}) / (3\lambda^2 I_D)$$
(5)

where  $\lambda = 1$  (channel length modulation);  $n_f$  depends on the ratio of transistors sizes;  $I_D$  is the current through each signal path.

# C. Signal conversion

In multi-stage analog operation, the accumulation of noise over multiple stages can cause significant degradation in SNR, to the point where the system may not be able to retain enough precision. Therefore, as described at the end of Section I, after a set of analog operations, we must restore the signals to the digital domain using an ADC [1]. After restoration, the computations can be performed in the digital domain or converted back to analog using a DAC.

1) ADC: The ADC energy is dependent on the effective number of bits (ENOB) [9], where ENOB is derived from the full-scale signal range (signal<sub>FS</sub>) and noise at the ADC input. For a *B*-bit ADC,

$$E_{\rm ADC} = K_1 \cdot \text{ENOB} + K_2 \cdot 4^{\text{ENOB}}$$
(6)

$$ENOB = \log_2 \left( \frac{RMS(signal_{FS})}{RMS(noise_{ADC}) \times \sqrt{12}} \right)$$
(7)

<sup>1</sup>As  $\tanh = (1 - e^{-2x})/(1 + e^{-2x})$  is a scaled and shifted form of sigmoid =  $1/(1 + e^{-x})$ , their energy and noise models are similar.

As the energy is proportional to ADC precision, we choose a minimum-precision ADC under the noise requirements. In convolution operations, since the ADC energy is shared across all filter elements, using a larger filter size can reduce the overall ADC energy. 2) DAC: We use a charge-distribution DAC [16], which also behaves as a sample-and-hold circuit (SHA). This saves chip area and power by removing the need for an external SHA. If  $C_u$  is the minimum realizable capacitance, the energy and the noise for a B-bit DAC are:

$$E_{\text{DAC}} = 2^B \alpha (C_u V_{DD}^2 + E_{switch}) \quad N_{\text{DAC}} = kT/(2^B C_u)$$

#### IV. NOISE PROPAGATION IN ML ARCHITECTURES

Based on the operations described in the previous section, we can model the energy and noise within each layer. Next, we consider noise propagation across layers. The weight distribution across layers in a deep neural network spans diverse numerical ranges [3]; therefore, a layer-wise quantization scheme improves the overall accuracy. We use the quantization noise arising from a uniform quantization scheme to explain how the noise is propagated through typical analog or digital operations in ML inference [20].

Digital noise. We use linear integer quantization noise for digital signals based on chosen bit precision. Quantization noise in each digital operator is assumed independent. After propagation over multiple operators, by the Central Limit Theorem, noise can be approximated as a normal distribution with zero mean/constant variance,  $\sigma^2$ .

Analog noise. This is calculated for each analog operation using noise equations (Section III-B), for a chosen equivalent bit precision. ADC/DAC noise is captured using methods from Section III-C.

Analog/Digital noise propagation. We show how the noise is propagated through some typical ML inference operations. Assuming noise at each layer weight to be independent with zero mean, if the input noise variances are  $\sigma_1^2$  and  $\sigma_2^2$  for a two-input operation (or just  $\sigma_1^2$  if unary), the output variance,  $\sigma^2$ , is:

• Add/Subtract: 
$$\sigma_1^2 + \sigma_2^2$$
 • Multiply:  $\sigma_1^2 \sigma_2^2$ 

• sigmoid [21]:  $\frac{\tan^{-1}(\sqrt{1+0.59\sigma_1^2})}{\pi} - \frac{1}{4}$  • ReLU:  $\sigma_1^2 / 2$ Consider the operation  $x_3 = x_1 + x_2$ . Let  $\sigma_{qx_1}^2 [\sigma_{qx_2}^2]$  be the variance of noise at input  $x_1 [x_2]$ . Let  $\sigma_{nx_3}^2$  be variance of the noise introduced by the addition operator. For addition in the digital [analog] domain,  $\sigma_{nx_3}^2$  represents the noise variance from the quantization of the adder [analog circuit nonidealities]. Since the total noise variance of the operation is the sum of all three variances, if  $\sigma_{x_3}^2$  is the signal power at the output, then the SNR at the output is:

$$SNR_o = \sigma_{x_3}^2 / (\sigma_{qx_1}^2 + \sigma_{qx_2}^2 + \sigma_{nx_3}^2)$$
(8)

Table I: LUT for analog/digital operations, at various precisions.

Operations	Analog Energy (fJ)							
Precision	1-bit	2-bit	3-bit	4-bit	5-bit	6-bit	7-bit	8-bit
ADC	100	200	300	400	501	624	747	885 [9]
Addition	2.5	4.0	6.5	10.0	14.5	20.0	26.5	34.0 [12]
DMAC	0.2	0.7	1.5	2.7	4.2	6.1	8.3	10.8 [9]
Max-pool	1	4	16	64	2.6e2	1.0e3	4.1e3	1.6e4 [18]
sigmoid	1	4	16	64	2.7e2	1.0e3	4.1e3	1.6e4 [19]
Operations	Digital Energy (fJ)							
Precision	1-bit	2-bit	3-bit	4-bit	5-bit	6-bit	7-bit	8-bit
DAC	0.5	1.0	2.0	4.0	8.0	16.0	32.0	64.0 [16]
Addition	9.5	12.5	15.4	18.3	21.2	24.1	27.0	30.0 [14]
DMAC	9.7	18.7	33.8	55.0	82.1	115.4	154.6	200 [14]
DMAC Max-pool	9.7 3.7e2	18.7 7.4e2	33.8 1.1e3	55.0 1.5e3	82.1 1.9e3	115.4 2.2e3	154.6 2.6e3	200 [14] 2.9e3 [14]



Figure 4: Inference performance of pre-trained ResNet18 trained on ImageNet dataset due to (a) quantization (b) added Gaussian noise with  $\sigma$  equivalent to bit-precision (one layer at a time).

# V. MISO-ML SETUP

**Energy lookup table.** The operations may be performed at a precision (or equivalent precision for analog computation) of 1–8 bits. Based on the models described previously, we generate a lookup table for energy and noise for each operation, as listed in Table I.

The energy for digital operations in Table I is based on a 12 nm node at  $V_{DD} = 1$ V and include the energy for memory read/write. We assume an activity factor  $\alpha = 0.1$ . The energy values for all bit precisions are derived by scaling the energy for 8-bit operations based on the number of bit operations, e.g., addition scales linearly and multiplication scales with the square of the number of bits.

For analog topologies, for any clock/data switching, we consider a switching energy of 2 fJ. For the energy model corresponding to 1bit precision, the minimum realizable capacitor  $(C_u)$  of 0.3fF. We set current  $(I_D)$  of 50 nA, temperature T = 300K,  $k = 1.38 \times 10^{-23}$  J/K, and channel length modulation  $\lambda = 1$ . To increase the precision by one bit under same the signal strength, noise must be reduced by half; this is achieved by quadrupling the capacitor sizes and current  $(I_D)$ . In Eq. (4) for the max-pooling operation,  $K' = 2.96 \times 10^{-20}$  as derived based on the circuit in [18] to achieve minimum energy, and in Eq. (5) for sigmoid,  $n_f = 1.5$ ,  $\Delta V = 0.1$ V [19].

For the ADC, we select the power numbers that correspond to the best ADC design for a given number of bits using [22], which gives  $K_1 = 100$  fJ,  $K_2 = 1$ aJ. For lower precision, we use successive-approximation-register (SAR) ADCs which use B + 1 cycles for computation. Based on the choice of capacitor sizes the ADCs can easily work up to 1 GHz, thus keeping the throughput of the model at 100 MHz ( $\approx 111$  MHz for an 8-bit ADC operation [16])

**Modeling error sensitivity.** We estimate digital noise using the quantization model from Section IV. Analog noise is modeled as white Gaussian noise with zero mean and variance  $= 1/2^{B}$  [1].

A pretrained model using 32-bit floating point (FP32) weights is used and layer-wise quantization is implemented. Fig. 4(a) shows the layer-by-layer analysis of the resilience of the ResNet18 model towards quantization. Quantization levels above 6-bit integers perform well, and these curves are not shown in the graph for enhanced readability. Below 6-bit quantization, we can see that the ResNet18 model has significant degradation in accuracy, though some accuracy can be regained after quantization-aware fine tuning of the model. A similar characteristic was observed while adding Gaussian noise to the weights of the model (Fig. 4(b)), but in this case, the network shows minimal degradation up to noise equivalent to 5bits ( $\sigma_{noise} = 1/32$ ). This shows that the ResNet18 model is more resilient to analog noise than to quantization loss.

We evaluate the *sensitivity* of the model  $S_j^t$ , indexed by the  $j^{\text{th}}$  operation of type t, as the ratio of the error of ML model to the added noise (analog Gaussian or digital quantization) for the operation. We will utilize these relative sensitivities of the added quantization and Gaussian noise in the ILP formulation described next.

Table II: ILP notation.

t	Operator type; $t \in O$
$O_j^t$	$j^{\text{th}}$ operator in the network of type t.
$ADC_B(DAC_B)$	<i>B</i> -bit ADC (DAC); $1 \le B \le 8$
$D_B^t(A_B^t)$	B-bit precision digital(analog) operator of type $t$
$I_j^X \in \{0,1\}$	If X is $A_B^t$ ( $D_B^t$ ), this indicator variable chooses variant X of $j^{\text{th}}$ operator, $O_j^t$ ; else if X is $ADC_B$ ( $DAC_B$ ), this indicates the presence(absence) of an $ADC_B(DAC_B)$ at output of $j^{\text{th}}$ operator, $O_j^t$ .
E(X)(N(X))	Energy consumed (Noise generated) by an operator $X$ in Table I.
$E_{ADC}^{total}(E_{DAC}^{total})$	Total energy consumed by all ADCs (DACs).
$S_j^t$	Noise sensitivity for $j^{\text{th}}$ operator of type $t$ .
FO(X)	the fan-out vertices of operator X
$N_T$	Noise threshold beyond which successive analog op- erations has to be succeeded by a digital operation

#### VI. MISO-ML PRECISION OPTIMIZATION

Consider an ML architecture composed of M layers, each of which performs one operation from the available set of operations {Addition, MAC, Max-pool, ReLU, sigmoid}. Each operation can have a precision of B bits,  $1 \le B \le 8$ , and can either be implemented using an analog or digital operation  $(O^t)$ ; if the output is very sensitive to an operation, it should preferably be performed using digital circuitry, but a less sensitive operation can be implemented in analog, using a noise threshold based on the desired precision to determine ADC insertion points (see "Intuitive concept," Section I). The set of allowable operations  $\mathcal{O}$  is all combinations of

{operation set, bit precision, implementation mode (analog/digital)} Our goal is to minimize the overall energy and noise in the system, trading off noise/energy using digital and analog components, and inserting ADCs/DACs as needed. Using the notation in Table II, we formulate an ILP to find the **bit-precision assignment**, the **choice of analog/digital** for each operation, and the **ADC/DAC locations**.

ILP Objective: We seek the best *compromise* in energy and noise as we solve the assignment problem. The objective function minimizes the sum of the overall energy consumed and noise generated (weighted by sensitivity  $S_j^t$ ) by all operators and ADCs/DACs, as represented in the optimization formulation below:

s.t

$$\min \sum_{j=1}^{M} \left( E(O_j^t) + S_j^t N(O_j^t) \right) + E_{\text{ADC}}^{\text{total}} + E_{\text{DAC}}^{\text{total}}$$
$$\sum_{B=1}^{8} \left( I_i^{A_B^t} + I_i^{D_B^t} \right) = 1$$
(9)

$$E(O_{j}^{t}) = \sum_{B=1}^{8} \left( I_{j}^{A_{B}^{t}} \cdot E(A_{B}^{t}) + I_{j}^{D_{B}^{t}} \cdot E(D_{B}^{t}) \right)$$
(10)

$${}^{ADC_B}_{j} = I_j^{A_B^t} \wedge \left(\bigvee_{k \in FO(j)} \left(\bigvee_{B=1}^{8} I_k^{D_B^k}\right)\right)$$
(11)

$$\left(\bigwedge_{k\in P} I_k^{A_{B_k}^t} \cdot \sum_{k\in P} N(A_{B_k}^t)\right) \cdot I_l^{D_{B_l}^t} \le N_T \tag{12}$$

$$E_{\text{ADC}}^{\text{total}} = \sum_{j=1}^{M} \sum_{B=1}^{8} I_j^{\text{ADC}_B} \cdot E(\text{ADC}_B)$$
(13)

The logical AND ( $\land$ ), OR ( $\lor$ ), and NOT ( $\overline{}$ ) operations in the ILP formulation can be easily modeled using ILP constraints [23].

Unique variant constraint: A special order set (SOS) constraint is formulated in (9) to choose one of the available variants (analog or digital, and a specific number of bits) for an ML layer.

Energy computation: With the above SOS representation, the energy consumed by an operator  $O_j^t$  (defined in Table II) can be evaluated as shown in (10). A similar expression represents the noise for  $O_j^t$ . <u>ADC/DAC constraint</u>: A *B*-bit ADC is required at the output of an analog operator of *B*-bit equivalent precision, whose output drives at least one operator that is digital, regardless of the digital precision. This is specified as the logical constraint (11). As described in Table II, operator  $O_i^t$  is an analog operator with *B*-bit equivalent precision if the indicator variable  $I_j^{A_B^{+}}$  is 1. At least one of the fanout operators of j is digital if any of the corresponding indicator variables of the digital variant of any precision is 1. This condition can be detected by ORing all such digital indicator variables as shown in (11). A similar constraint is included for DAC indicator variables when a digital operator drives one or more analog operators.

<u>Noise threshold constraint</u>: The SNR may degrade significantly when multiple analog operators are cascaded. To prevent this, a chain of analog operators must be followed by a digital operator to restore signals to discrete values, as described in Section III-C. To specify this constraint, consider a path P in the network comprising successively adjacent operators, whose last operator drives a digital operator l. Any path composed of all-analog operators must have an accumulated noise of less than  $N_T$ . All the operators in a path are analog if and only if the analog indicator variables of all operators in the path are 1, which is captured by an AND constraint. A  $B_k$ -bit precision for operator  $k \in P$  is specified as shown in (12).

The ILP solution assigns to each operator a bit-precision and analog/digital variant based on the indicator variable. An ADC/DAC is added to the output of an operator if its indicator variable is 1.

# VII. EVALUATION OF MISO-ML

We demonstrate our approach on multiple ML architectures. **ResNet18 with ImageNet.** We first apply our approach on ResNet18 with a workload from the ImageNet 1k dataset. Our ILP solution provides the bit-precision, choice of analog/digital implementation, and the locations and bitwidths of the ADCs/DACs corresponding to the optimal noise and minimum energy. We compare this with a reduced bitwidth digital optimization, i.e., digital quantization.

Table III shows energy and quantization numbers corresponding to uniform digital quantization across all layers of ResNet18 on the ImageNet dataset. Models with uniform 8-bit quantization achieve similar accuracy compared to the baseline FP32 model. The use of 6-bit and 4-bit uniform quantization sees some accuracy drop, which is recovered after retraining, accounting for quantization and analog noise (*"fine tuning"*). However, for 2-bit uniform quantization, the accuracy degrades greatly and cannot be recovered by fine tuning.

 Table III: Energy vs top-1 accuracy trade-off for ResNet-18 architecture on the ImageNet dataset.

Precision	Acc	uracy	Energy
(D) = Digital, (A) = Analog	Inference	Fine tuning	(Improvement)
FP32 (D)	69.57%	-	-
8B Activation, 8B Weight (D)	69.49%	69.49%	25.62µJ (1.00×)
6B Activation, 6B Weight (D)	68.43%	69.21%	18.74µJ (1.37×)
4B Activation, 4B Weight (D)	66.82%	68.66%	12.32µJ (2.08×)
2B Activation, 2B Weight (D)	62.14%	65.38%	6.18µJ (4.14×)
MiSO-ML (4/6B Activation, 4/6B Weight (mix))	67.14%	69.16%	3.14µJ (8.16×)

The MiSO-ML mixed precision method, with mixed analog/digital implementations with cascaded analog MAC structures, uses  $6 \times$  less energy than 6-bit uniform quantization, which provides the same accuracy. Relative to [9], [13], which use ADCs between successive layers, the benefit of MiSO-ML comes due to *explicit optimization* of the number of ADCs between multiple analog stages: since ResNet uses convolution filters of size  $3 \times 3$  for all of the convolution stages (except the first convolution layer with  $7 \times 7$  filter size), the ADC energy cost becomes a significant portion of MAC energy in [9], [13].

The results of optimizing ResNet18 on ImageNet using MiSO-ML are shown in Fig. 5. For each layer (1–18 on the x-axis), the weights are always digital; depending on the ILP optimization, the activations and operation may be digital ("D") or analog ("A"). The bars show the equivalent number of bits (if analog) or truncated bits (if digital) for

the weights, activations, and operation, according to the left y-axis. The ILP places data converters at layers 6, 9, 13, and 17.

The green line shows the energy reduction per layer (right yaxis) as compared to a 6B digital implementation, which has similar accuracy (Table III). Layers with analog operations provide large energy reductions; those with digital operations (1, 17, 18) less so, but maintain accuracy. For a threshold noise of  $\sigma_{max}(N_T) = 1/20, 2$  to 3 layers can be stacked in the analog domain before data conversion. Accuracy vs. energy tradeoffs. For the same experimental setup (ResNet18 on ImageNet), Fig. 6 shows the energy vs. accuracy tradeoff for different noise thresholds for MiSO-ML, and with equivalent bit truncation for a digital implementation. We see a large energy improvement by the MiSO-ML model for lower bit precisions, and more modest improvement for digital truncation. The accuracy cost is minimal up to 4-bit precision but is more noticeable for a lower number of bits. Using this energy vs. accuracy tradeoff curve, we select 4-bit precision, and this limits the AND constraints in the ILP. Benefit of stacking analog operations. To understand the benefit of stacking multiple layers before ADC insertion, we plot the percentage contribution of the ADCs to the overall energy in Fig. 7. We assume that the input and output layers of the ML architecture are in the digital domain. The yellow bars correspond to the MiSO-ML architecture with ADCs inserted based on the ILP, and the gray bars correspond to the operations at a bit precision optimized in MiSO-ML, but with an ADC/DAC after each ML layer, similar to [9], [13]. The energy gain is considerable for 4-6 bit operations as compared to 7-8 bit operations. At stricter 7- and 8-bit precision, smaller benefits from analog operations are seen, due to high ADC/DAC energy costs.

The improved benefit of analog operation at 6-bits and below is attributed to the amortization of the cost of ADC and DAC over a stack of multiple layers; this is less so at 7–8 bits. We observe a stacking of up to two layers for a 6-bit equivalent precision and a stacking of up to four layers for a 4-bit equivalent precision. At 3-bit and lower precision, we do not observe any significant reduction of ADC energy component due to reduced energy scaling for the ADC operation, as seen in Table I. For a 4-bit noise threshold, the ADC energy overhead is just 13.2% of the total energy of ResNet18, much smaller as compared to single-layer architectures (52.2% in [11]). **General ML Architectures.** We have tested various networks and observed consistent improvement across all. In Table IV, we describe the energy efficiency achieved by our model on multiple ML architectures. We chose four datasets to test our model: MNIST (using image-



Figure 5: Equivalent number of bits for all ResNet18 layers. Data converters are placed at the shaded layers (6,9,13,17).



Figure 6: MiSO-ML energy vs. accuracy trade-off plot for different noise threshold constraints for the ResNet18 architecture using an ImageNet workload. MiSO-ML energy improvement (gray columns) is nonlinear while digital energy improvement is modest (yellow bars).



Figure 7: ADC energy (% of total energy) vs. noise threshold constraints for ResNet18. Gray bars: ADC inserted after each layer [9].

Table IV:	Energy	reduction	and	accuracy	for	different i	methods.
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Dataset	ML Architecture	Accurac	Energy/inference	
MNIST	SVM (Accuracy = 94.23%)	MiSO-ML	92.31%	0.16µJ (3.16×)
ImageNet	ResNet18 (Accuracy = 69.57%)	BitBlade [6] MiSO-ML	68.66% <b>69.16%</b>	15.8μJ (1.64×) <b>3.14</b> μJ ( <b>8.16</b> ×)
Imagenette	VGG16 (Accuracy = 92.32%)	MiSO-ML	90.51%	8.48µJ (7.69×)
	GoogLeNet (Accuracy = 93.23%)	MiSO-ML	91.46%	2.56µJ (6.25×)
	ResNet101 (Accuracy = 96.55%)	MiSO-ML	93.76%	5.08µJ (9.12×)
CIFAR-10	PasNat20 (Accuracy = 91.12%)	AA-ResNet [7]	80.90%	<b>0.6</b> µJ (5.76×)
	Residence (Recuracy = 91.12 %)	MiSO-ML	87.25%	0.66µJ (5.52×)
	ResNet110 (Accuracy = 93.55%)	MiSO-ML	92.55%	2.89µJ (5.56×)

(a subset of ImageNet with 10 classes using image-pixel 112×112), and CIFAR-10 (using image-pixel 32x32). The Baseline architecture is an 8-bit digital implementation of the ML architecture. Based on our energy vs. accuracy tradeoff (Fig. 6), we target a maximum degradation of 5%, i.e.,  $\sigma_{noise} = 1/20$  for the ILP. For the MNIST dataset, there exists a large literature of binary classifiers [3], [4] that can achieve better accuracy, but considering our objective of energy efficiency we choose a simple SVM classifier. We achieve minimal degradation with a 6-bit SVM classifier. Our optimization provides a  $3.16\times$  energy efficiency as compared to the digital implementation.

For ImageNet, the table shows MiSO-ML on ResNet18, and also 4bit optimized digital hardware [6] (with energy scaled from 28nm to 12nm). MiSO-ML can achieve higher energy improvement through mixed-signal implementation and bit-width optimization.

For Imagenette [24], we evaluate MiSO-ML on three architectures – VGG16, GoogleNet, and ResNet101 – and achieve considerable energy efficiency. This shows that our method can be extended to a large number of ML architectures. VGG16 is highly computationintensive and consists of 38.7G MAC, 49.21M pool, 100 add, 100 div, and 100 exp operations. GoogleNet uses an inception module with convolutions of different sizes and consists of 4.01G MAC, 40.26M pool, 2.21M add, 4.16M div, and 2.8M exp operations. ResNets use residual blocks to overcome the vanishing gradient problem in previous architectures and allow the stacking of a large number of convolution layers varying from 18 up to 1202. ResNet101 consists of 1.93G MAC, 5.44M pool, 8.11M add, 5.29 div, and 10 exp operations.

We apply the MiSO-ML strategy on ResNet architecture and the CIFAR-10 dataset and observe a similar trend. The ResNet architectures for the CIFAR-10 dataset do not contain a max-pool layer at the beginning. We observed that the impact of adding noise is lower for the initial layers of the architecture. Since the number of convolution operations decreases faster in ResNet-Imagenette layers than in ResNet-CIFAR-10 layers, the impact of energy benefit due to low bit-analog operations is significant. This explains the  $8.16 \times$  energy improvement for ResNet18-ImageNet as compared to  $5.52 \times$  improvement for ResNet20-CIFAR-10. We compare our results against a 4B Weight, 7B Activation analog implementation [7] and observe that we can achieve much higher accuracy with a mixed signal approach with minimal increase in energy.

The ILP size depends on the size of the ML model and the number of possible bit-precisions. We use Gurobi [25], which solves the ILP in less than a minute for ResNet18 and 35 minutes for ResNet101 on an Ubuntu host with a 2.6GHz Intel Core i7 processor and NVIDIA Quadro P620 GPU. The runtime of MiSO-ML is very small compared to the full training for these models which run for multiple days.

# VIII. CONCLUSION

We propose MiSO-ML, a mixed-signal optimization framework for low-power ML inference. We demonstrate that it can enable image recognition for multiple ML architectures. We observe a gain of  $5-8\times$  lower energy than 8-bit quantized digital implementations, with minimal accuracy loss. The main energy benefit comes from the low ADC energy (13.2%, amortized across multiple layers) and selection of energy-efficient analog/digital hardware for different precisions. The ILP formulation ensures that accuracy loss is minimal.

#### REFERENCES

- R. Sarpeshkar, "Analog versus digital: Extrapolating from electronics to neurobiology," *Neural Computation*, vol. 10, pp. 1601–1638, 1998.
   K. Boahen, "A neuromorph's prospectus," *Computing in Science &*
- [2] K. Boahen, "A neuromorph's prospectus," Computing in Science & Engineering, vol. 19, pp. 14–28, 2017.
- [3] Z. Yao, et al., "HAWQV3: dyadic neural network quantization," arXiv:2011.10680, 2020.
- [4] A. Agrawal, et al., "Approximate computing: Challenges and opportunities," in Proc. ICRC, pp. 1–8, 2016.
- [5] S. Han, et al., "Deep compression: Compressing deep neural network with pruning, trained quantization and Huffman coding," in Proc. ICLR, 2016.
- [6] S. Ryu, et al., "Bitblade: Energy-efficient variable bit-precision hardware accelerator for quantized neural networks," *IEEE J. Solid-St. Circ.*, pp. 1924–1935, 2022.
- [7] J. Lim, et al., "AA-ResNet: Energy efficient all-analog ResNet accelerator," in Proc. MWSCAS, pp. 603–606, 2020.
- [8] C. Zhou, et al., "AnalogNets: ML-HW co-design of noise-robust tinyml models and always-on analog compute-in-memory accelerator," arXiv:2111.06503, 2021.
- [9] B. Murmann, "Mixed-signal computing for deep neural network inference," *IEEE T. VLSI Syst*, vol. 29, pp. 3–13, 2021.
- [10] A. S. Rekhi, et al., "Analog/mixed-signal hardware error modeling for deep learning inference," in Proc. DAC, 2019.
- [11] S. Ghodrati, et al., "Mixed-signal charge-domain acceleration of deep neural networks through interleaved bit-partitioned arithmetic," in Proc. PACT, pp. 399–411, 2020.
- [12] B. Sadhu, et al., "Analysis and design of a 5 GS/s analog charge-domain FFT for an SDR front-end in 65 nm CMOS," *IEEE J. Solid-St. Circ.*, vol. 48, pp. 1199–1211, 2013.
- [13] M. Kang, et al., "A multi-functional in-memory inference processor using a standard 6T SRAM array," *IEEE J. Solid-St. Circ.*, vol. 53, pp. 642–655, Feb. 2018.
- [14] M. Horowitz, "Computing's energy problem (and what we can do about it)," in *Proc. ISSCC*, pp. 10–14, 2014.
- [15] U. Vishnoi and T. G. Noll, "Area-and energy-efficient CORDIC accelerators in deep sub-micron CMOS technologies," Advances in Radio Science, vol. 10, pp. 207–213, 2012.
- [16] B. Razavi, Design of Analog CMOS Integrated Circuits. New York, NY, USA: McGraw-Hill, Inc., 2001.
- [17] E. H. Lee and S. S. Wong, "Analysis and design of a passive switchedcapacitor matrix multiplier for approximate computing," *IEEE J. Solid-St. Circ.*, vol. 52, pp. 261–271, 2017.
- [18] J. Choi, et al., "Design of an always-on image sensor using an analog lightweight convolutional neural network," MDPI Sensors Journal, vol. 20, 2020.
- [19] S. Sadasivuni, *et al.*, "Fusion of fully integrated analog machine learning classifier with electronic medical records for real-time prediction of sepsis onset," *Scientific Reports*, vol. 12, p. 5711, 2022.
- [20] B. Jacob, *et al.*, "Quantization and training of neural networks for efficient integer-arithmetic-only inference," in *Proc. CVPR*, pp. 2704– 2713, 2018.
- [21] J. Daunizeau, "Semi-analytical approximations to statistical moments of sigmoid and softmax mappings of normal variables," *arXiv*:1703.00091, 2017.
- [22] B. Murmann, "ADC performance survey 1997-2022." http://web. stanford.edu/~murmann/adcsurvey.html, 2022.
- [23] J. Hooker and M. Osorio, "Mixed logical-linear programming," Discrete Applied Mathematics, vol. 96-97, pp. 395–442, 1999.
- [24] J. Howard, "Imagenette." https://github.com/fastai/imagenette/.
- [25] Gurobi Optimization, "Gurobi Optimizer Reference Manual," 2022.