## EE5585: Homework 4

All problems carry equal points. Due date: May 9 (before class starts)
(1) Suppose $Z_{1}$ and $Z_{2}$ are iiid $\operatorname{Bernoulli}(p)$ random variable, i.e. $\operatorname{Pr}\left(Z_{1}=\right.$ $1)=p=\operatorname{Pr}\left(Z_{2}=1\right)$. Say $X_{1}=Z_{1}+Z_{2}$ and $X_{2}=Z_{1} Z_{2}$ are two random sources that are seen by Alice and Bob respectively. What is the achievable rate limits of the distributed data compression for $X_{1}$ and $X_{2}$ sequences in this case?
(2) Following table shows height-weight data of 12 monkeys:

| Height | Weight |
| :---: | :---: |
| 18 | 29.5 |
| 28 | 39.2 |
| 36 | 54.5 |
| 25 | 36.0 |
| 17 | 25.0 |
| 31 | 43.8 |
| 21 | 30.4 |
| 35 | 56.1 |
| 24 | 36.0 |
| 22 | 29.9 |
| 18 | 26.9 |
| 32 | 48.2 |

Find out the Karhunen-Loeve transform matrix to compress this data. Perform PCA.
(3) Assume the range of Height in the data of problem 2 is $[18,36]$ and for weight $[25,57]$. Design a 2 -bit vector quantizer for this data. What would be the 1-bit scalar quantizer for each column? Find out error for the given data for both the quantizers (scalar and vector).

